

# Cortical network dynamics with time delays reveals functional connectivity in the resting brain

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**Abstract** In absence of all goal-directed behavior, a characteristic network of cortical regions involving prefrontal and cingulate cortices consistently shows temporally coherent fluctuations. The origin of these fluctuations is unknown, but has been hypothesized to be of stochastic nature. In the present paper we test the hypothesis that time delays in the network dynamics play a crucial role in the generation of these fluctuations. By tuning the propagation velocity in a network based on primate connectivity, we scale the time delays and demonstrate the emergence of the resting state networks for biophysically realistic parameters.

**Keywords** Resting brain · Default mode

## Introduction

The primate brain exhibits spontaneous coherent fluctuations in absence of all environmental stimuli and goal

directed behavior (Biswal et al. 1995; Gusnard and Raichle 2001; Fox et al. 2005; Greicius et al. 2003; Damoiseaux et al. 2006; Vincent et al. 2006; Bar 2007). These fluctuations primarily occur in a network consisting of prefrontal, parietal and cingulate cortices. In humans, this network has been shown to greatly overlap with functional architectures present during consciously directed activity and hence various functional roles such as “day-dreaming” or “stimulus-independent thought” have been attributed to it. Just recently it has been put forward that the transient resting state activations are reminiscent of features of a more fundamental organization of the cortex. This proposal has been motivated by the identification of the presence of similar resting state networks in monkeys during deep anaesthesia (Vincent et al. 2007). In the present paper, we put this hypothesis to test and investigate if a neural network dynamics with realistic primate connectivity and time delays is capable of generating the coherent rest state fluctuations. The introduction of time delays is well motivated, since we deal with large-scale connectivity (Jirsa 2004) involving far distant brain areas.

## Anatomical connectivity analysis

The basis of our network is the connectivity matrix of one hemisphere obtained from the CoCoMac database (Kötter 2004). This primate anatomical connectivity matrix (colated from macaque tracing studies) comprises 38 nodes with weights ranging from 0 to 3. The corresponding “Regional map” gives the translation between macaque and human neuroanatomy (Kötter 2005). To quantify the connectivity characteristics, we computed a set of network connectivity measures (Honey et al. 2007) for all nodes including the in- and out-degree of connectivity and the

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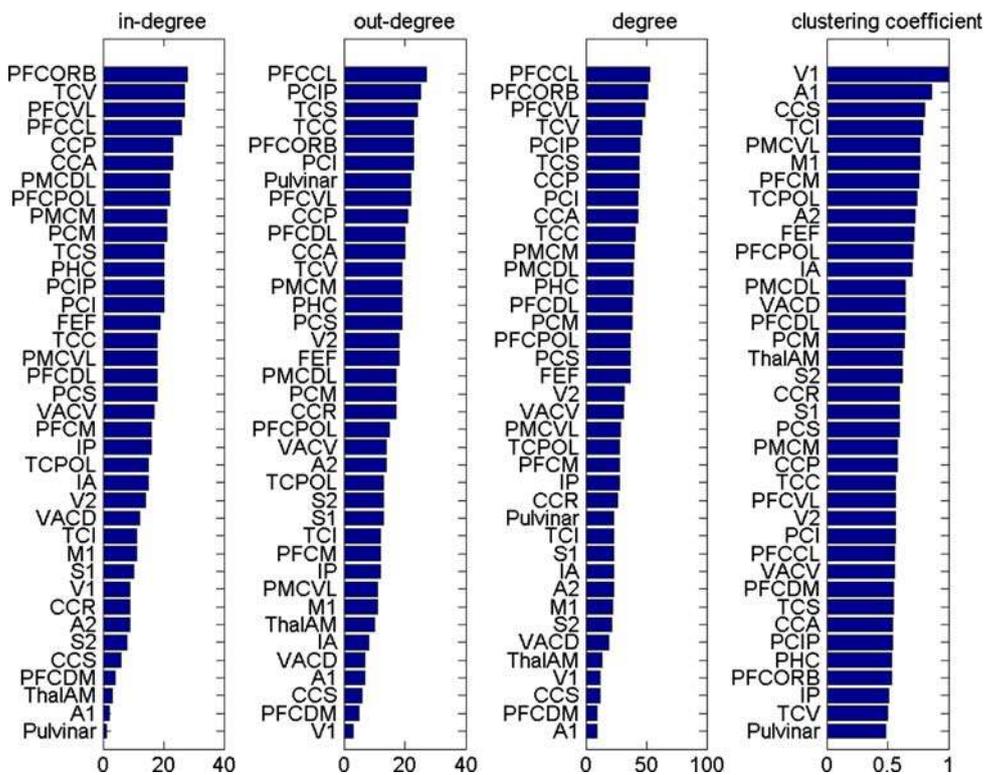
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**Fig. 1** Characterization of the primate connectivity matrix: node wise degree distributions and clustering index



clustering coefficient (see Fig. 1). The in-degree and out-degree are computed as the number of incoming and outgoing connections to/from a node, respectively, giving a measure of how much information it can receive or give. The degree is the sum of in- and out-degree. The clustering coefficient is calculated as the number of all existing connections between a node’s neighbors divided by all such possible connections. The connection graph has 599 edges, with connection density = 0.426, characteristic path length = 1.633 and clustering index = 0.568.

Our analysis shows that the components of the rest state network are not clearly differentiated from other network nodes. Anatomically the prefrontal cortex is characterized by a large degree of afferent and efferent connectivity, whereas cingulate and parietal areas display only a moderate degree of connectivity. Clustering index is commonly used to identify hubs in a network, but does not differentiate the default network either. Previous anatomical analyses evaluating whether the correlation between spontaneous rest activity and its underlying anatomical circuitry is high were based on retrograde tracer injection studies (Vincent et al. 2007); these trace out the direct afferent connectivity of a region of interest, i.e., the injection site, but are not able to provide insight into the large scale network connectivity. Our results suggest that an anatomical connectivity analysis of the large-scale network does not suffice to identify the network

constituents during rest, but rather requires an analysis of the network dynamics.

**Functional connectivity analysis**

To explore the network dynamics supported by the present large-scale connectivity matrix, we simulated the network dynamics computationally. We placed neuronal oscillators at each network node and initially considered multiple oscillator types which are commonly used in neural population modeling including Hopf oscillators (Breakspear and Jirsa 2007), Wilson–Cowan (Wilson and Cowan 1972) and FitzHugh–Nagumo (FitzHugh 1961; Nagumo et al. 1962) systems. Since all neural oscillators provided similar results, we present in the following the simulations based upon FitzHugh–Nagumo systems representing neural population activity (see also Assisi et al. 2005 for population modeling). Each network node was characterized by a degree of excitability, in which the increase of excitation parameterizes the onset of oscillations emerging from a quiescent state. Then the network node equations are given as

$$\dot{u}(t) = g(u, v) = \tau \left[ v + \gamma u - \frac{u^3}{3} \right]$$

$$\dot{v}(t) = h(u, v) = -(1/\tau)[u - \alpha + bv - I]$$

where  $u$  and  $v$  represent the fast and slow variables respectively (Breakspear and Jirsa 2007). The network model equations are given by:

$$\dot{u}_i(t) = g(u_i, v_i) - \sum_{j=1}^N f_{ij} u_j(t - \Delta t_{ij})$$

$$\dot{v}_i(t) = h(u_i, v_i)$$

where  $f$  represents the connection matrix of dimension  $N \times N$  (scaled by the value 0.016 to ensure dynamic stability),  $N$  being the number of nodes and the time delays are computed from the distance matrix  $d$  and  $v$  is the propagation velocity,

$$\Delta t_{ij} = \frac{d_{ij}}{v}$$

The simulations are carried out for transient rest state dynamics i.e., there is no external stimulus,  $I = 0$ , and the network dynamics evolves from a random initial condition to its stable equilibrium point. This transient dynamics is typically complex and involves oscillatory behavior, which we do not characterize in more detail in the current study. Here our only concern is the measurement of the spatial network configurations activated during this transient. The parameter values are set as follows:  $\alpha = 1.05$ ,  $b = 0.2$ ,  $\gamma = 1.0$ ,  $\tau = 1.25$ . We employed Matlab DDE23 for numerical integration. We set the propagation velocity,  $v$ , to multiple biologically realistic values and its infinite value.

To characterize the functional connectivity of this network, we apply a set of spatiotemporal measures. The first measure we apply is the integrated entropy (Tononi and Edelman 1998). Let  $u(i)$  be the temporal data at  $i$ th node (in our case the fast variables from the FitzHugh–Nagumo system) and we compute the joint probability distribution  $p(u(i), u(j))$  and the entropy is obtained by

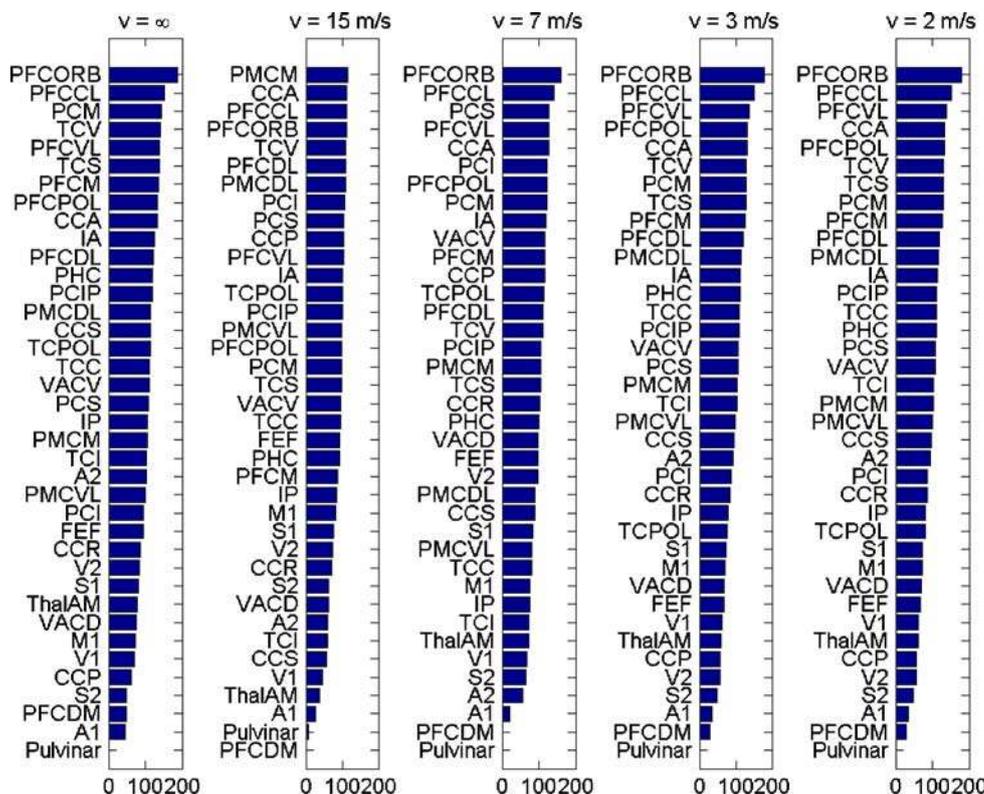
$$H(i, j) = - \sum_{i=1}^N \sum_{j=1}^N p(u(i), u(j)) \log[p(u(i), u(j))].$$

Thus we obtain the entropy matrix of dimension  $N \times N$ , where  $N$  is the number of nodes in the connectivity matrix. To quantify the entropy contribution of each node we calculate the row or column sum ( $H$  being a symmetric matrix)

$$H(i) = \sum_{j=1}^N H(i, j).$$

The above quantity is known as integrated entropy, signifying statistical independence of a particular area ( $i$ ) in the network from others and is shown in Fig. 2 for the velocity values  $\infty$ , 15, 7, 3, and 2 m/s. We find that for instant transmission, i.e., infinitely large velocity, the prefrontal areas (PFCORB, PFCCL) show higher integrated entropy compared to the rest of the nodes while for finite velocities there emerge links to anterior cingulate (CCA) and other areas, in particular also to CCP

**Fig. 2** Integrated entropy for transmission speeds  $\infty$ , 15, 7, 3, and 2 m/s





$$C_{p,q} = Cov(W_{jm}^p, W_{jm}^q)$$

In Fig. 4 we show the thresholded covariance matrix, where the threshold has been chosen as  $c_{th} = 0.15$  and dark spots have strength greater than  $c_{th}$ . The threshold is chosen such that entries in the connectivity matrix lie outside the standard deviation calculated for all elements in the covariance matrix,  $C$ . The covariance matrix clearly indicates that the functional subnetwork in resting state is cingulate–prefrontal and medial premotor in nature. Similar analysis for low velocities yield only a single dominating entry namely PFCORB, indicating the other areas are implicated for higher velocity regimes.

## Conclusions

For increasing transmission speed the sub-networks present in transient rest state activity disengage the cingulate components and are left with only its prefrontal contributions for instantaneous transmission, thus resembling characteristics of anatomical connectivity. Hence we find evidence that the introduction of time delays aids in the additional recruitment of cingulate cortex. This suggests that the space–time structure of the time delays is crucial for the understanding of the brain’s rest state. In fact, our results demonstrate that the correlation structure of the rest state networks previously observed in experiments can be understood on the basis of the spatial (anatomical connectivity) and temporal (time delays) properties of connectivity. Our findings are consistent with the proposal that coherent spontaneous fluctuations of the resting brain reflect a more fundamental or intrinsic property of functional organization of the human brain (Jirsa 2004); not exclusively dependent on the presence of conscious mental activity.

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## Appendix: list of cortical areas

A1	Primary auditory
A2	Secondary auditory
CCA	Anterior cingulate cortex
CCP	Posterior cingulate cortex
CCR	Retrosplenial cingulate cortex
CCS	Subgenual cingulate cortex
FEF	Frontal eye field
IA	Anterior insula
IP	Posterior insula

M1	Primary motor cortex
PCI	Inferior parietal cortex
PCIP	Intraparietal sulcus cortex
PCM	Medial parietal cortex
PCS	Superior parietal cortex
PFCCL	Centrolateral prefrontal cortex
PFCDL	Dorsolateral prefrontal cortex
PFCDM	Dorsomedial prefrontal cortex
PFCM	Medial prefrontal cortex
PFCORB	Orbital prefrontal cortex
PFCPOL	Prefrontal polar cortex
PFCVL	Ventrolateral prefrontal cortex
PHC	Parahippocampal cortex
PMCDL	Dorsolateral premotor cortex
PMCM	Medial (supplementary) premotor cortex
PMCVL	Ventrolateral premotor cortex
S1	Primary somatosensory cortex
S2	Secondary somatosensory cortex
TCC	Central temporal cortex
TCI	Inferior temporal cortex
TCPOL	Polar temporal cortex
TCS	Superior temporal cortex
TCV	Ventral temporal cortex
V1	Primary visual cortex
V2	Secondary visual cortex
VACD	Dorsal anterior visual cortex
VACV	Ventral anterior visual cortex
Pulvinar	Pulvinar
ThalAM	Anteromedial thalamus

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