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## Crossed-beam energy transfer in direct-drive implosions<sup>a)</sup>

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Direct-drive-implosion experiments on the OMEGA laser [T. R. Boehly *et al.*, *Opt. Commun.* **133**, 495 (1997)] have showed discrepancies between simulations of the scattered (non-absorbed) light levels and measured ones that indicate the presence of a mechanism that reduces laser coupling efficiency by 10%–20%. This appears to be due to crossed-beam energy transfer (CBET) that involves electromagnetic-seeded, low-gain stimulated Brillouin scattering. CBET scatters energy from the central portion of the incoming light beam to outgoing light, reducing the laser absorption and hydrodynamic efficiency of implosions. One-dimensional hydrodynamic simulations including CBET show good agreement with all observables in implosion experiments on OMEGA. Three strategies to mitigate CBET and improve laser coupling are considered: the use of narrow beams, multicolor lasers, and higher-Z ablaters. Experiments on OMEGA using narrow beams have demonstrated improvements in implosion performance. © 2012 American Institute of Physics. [<http://dx.doi.org/10.1063/1.4718594>]

### I. INTRODUCTION

The direct-drive approach to inertial confinement fusion (ICF)<sup>1,2</sup> is based on the implosion, compression, and subsequent ignition of mm-diameter cryogenic deuterium–tritium (DT) ice shell targets using high-intensity ( $I \sim 10^{14}$ – $10^{15}$  W/cm<sup>2</sup>) lasers irradiation [Fig. 1(a)]. Direct drive offers the possibility of higher gain than indirect-drive implosions of the same laser energy.<sup>4</sup> To validate physics effects in direct-drive-ignition experiments planned for the National Ignition Facility (NIF),<sup>5</sup> the experiments are carried out on the OMEGA Laser System<sup>6</sup> that employs 60 laser beams with a total energy up to 30 kJ [Figs. 1(b) and 1(c)]. Experiments to study ignition-relevant conditions require a laser energy  $\sim 1$  MJ and will be conducted on the NIF in the polar-drive configuration.<sup>7</sup>

High-intensity incident light is absorbed in a corona of direct-drive targets, and the released heat drives the implosions by ablating the outer target surface. The dominant absorption mechanism on the OMEGA and NIF lasers, which operate on a wavelength  $\lambda_L = 351$  nm, is inverse-bremsstrahlung or “collisional absorption.”<sup>8</sup> Laser light is absorbed in a relatively narrow radial region with electron densities  $n_e$  from  $\sim 0.5$  to  $1 n_{cr}$ , where  $n_{cr} = \pi c^2 m_e / \lambda_L^2 e^2 \approx 9 \times 10^{21}$  cm<sup>-3</sup> is the critical density,  $m_e$  is the electron mass,  $e$  is the electron charge, and  $c$  is the speed of light. The symmetric illumination of targets with many laser beams, crossing each other at different angles and directions, creates conditions for transferring

energy among beams because of electromagnetic-seeded, low-gain stimulated Brillouin scattering (SBS).<sup>9</sup> Figure 2 illustrates the geometry of crossing rays when the most-efficient energy transfer occurs at the radii outside the highest absorption region with  $n_e$  from  $\sim 0.1$  to  $0.5 n_{cr}$ . The outgoing edge-beam light in beam 1 seeds perturbations to the incoming center-beam light in beam 2 (Fig. 2), scattering this light outward. Because of this scattering, the incoming light fails to penetrate into the most-absorbing region of the corona (where  $n_e \sim n_{cr}$ ) and deposit its energy there, as it does without scattering, reducing laser coupling. Calculations show that crossed-beam energy transfer (CBET) becomes important in OMEGA implosions at intensities  $I \gtrsim 10^{14}$  W/cm<sup>2</sup>.

It was realized almost four decades ago in the ICF community that simulations utilizing the Spitzer-Härm heat transport model<sup>10</sup> significantly overpredict the laser drive. To fix this problem, a limitation of the Spitzer-Härm fluxes were proposed, using an adjusting flux-limiter parameter  $f \approx 0.04 - 0.1$ .<sup>11</sup> Although no physical justifications of this approach were provided, it gave a reasonably accurate representation of the experiments (with some caveats, however, regarding measured scattered-light spectra), which were routinely performed last decades on OMEGA and include planar shock-timing experiments<sup>12</sup> and implosions using 1-ns square laser pulses at intensities  $I \sim 10^{14} - 10^{15}$  W/cm<sup>2</sup>. It was found more recently, however, that implosions performed at different conditions (with longer square or shaped pulses) cannot be accurately modeled using fixed or time-dependent  $f$ . This is because the simulations, in a general case, can be adjusted by varying  $f$  to match only one observable (e.g., the absorption fraction) leaving unmatched other observables

<sup>a)</sup>Paper Y13 1, *Bull. Am. Phys. Soc.* **56**, 360 (2011).

<sup>b)</sup>Invited speaker.

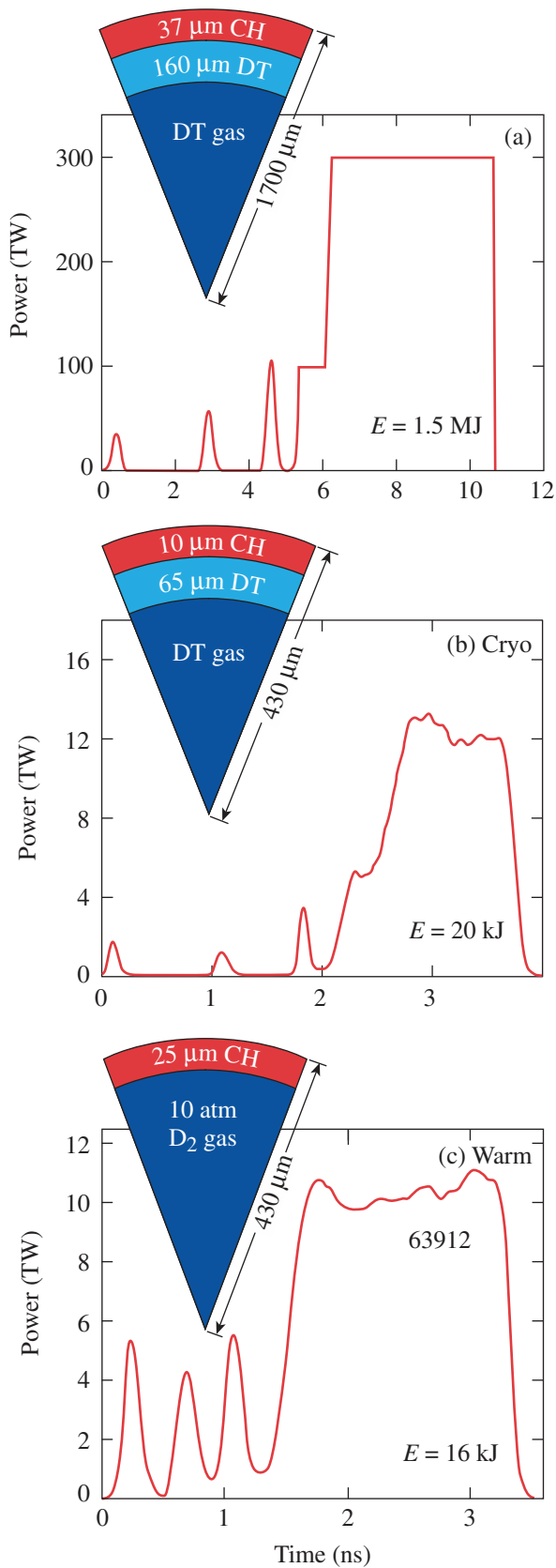


FIG. 1. (a) A 1.5-MJ direct-drive NIF ignition design.<sup>3</sup> This design utilizes a triple-picket pulse and releases an energy gain of about 50. (b) Typical cryogenic OMEGA target. This target is a scaled-down version of the design in (a) and optimized for a laser energy up to 30 kJ. (c) Example of a warm OMEGA target (shot 63912). Such targets are a less-expensive alternative to cryogenic OMEGA targets. The warm targets are used to study laser coupling, hydrodynamic stability, hot-spot formation, and other aspects of implosion physics.

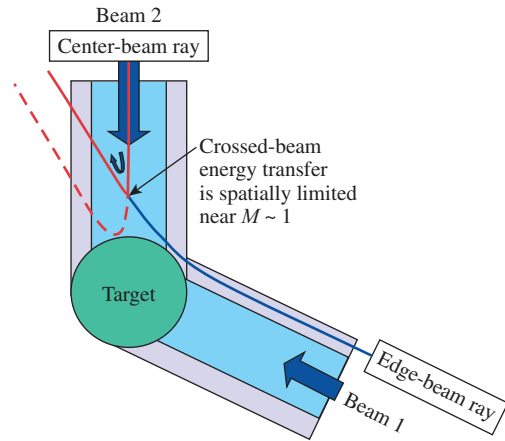


FIG. 2. Schematic illustration of a laser-ray geometry with the most energetically efficient CBET in a corona of an implosion target. An incident edge-beam ray (shown in blue) in beam 1 is refracted and turned outward above the critical radius. On its outgoing trajectory, this ray seeds perturbations to an incoming center-beam ray (shown in red) in beam 2 that results in energy transfer from the latter ray to the outgoing ray (also shown in red). The energy transfer occurs near the Mach 1 radius, which is typically located at  $n_e$  from 0.2 to 0.3  $n_{cr}$ . As the result of CBET, center-beam rays deliver less energy to the maximum absorption region near the critical radius.

(e.g., the bang time). To resolve this problem, the flux-limited model is substituted by a recently developed nonlocal heat transport model,<sup>13</sup> which utilizes a solution of the simplified Boltzmann equation without assuming the small mean free-path for electrons. This nonlocal model provides good agreements in the wide range of experimental conditions.

Figure 3 illustrates the discrepancy between the modeled scattered-light power (i.e., the difference between the incident and absorbed powers) without CBET in a plastic-shell (CH) implosion driven at  $I = 4.5 \times 10^{14}$  W/cm<sup>2</sup> and experimental observations. The green dashed-dotted and blue short-dashed lines in Fig. 3 show simulated powers using flux-limited (with  $f = 0.06$ ) and nonlocal transport models, respectively. These simulations significantly underestimate and are not able to correctly reproduce the measured power<sup>14</sup> shown by the black thick solid line in the same

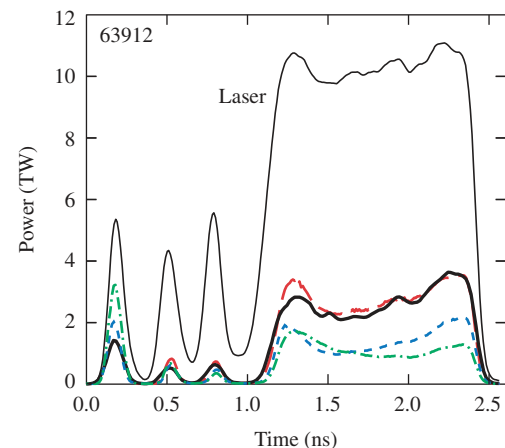


FIG. 3. Reflected light power history measured (thick black line) and simulated using flux-limited transport (green dashed-dotted line), nonlocal transport (blue short-dashed line), and nonlocal transport with CBET (red long-dashed line). The thin black line shows the incident laser power. Note good agreement between the measured power history and the simulated one with CBET.

figure. The simulations overpredict the measured absorption by about 10%. Simulations of the same implosion but including CBET, however, accurately reproduce the measurements (compare long-dashed and solid lines in Fig. 3). Simulations including CBET show good agreement with all observables in implosion experiments using different laser energies, pulse shapes, and targets. Examples of these simulations are discussed in Ref. 15 with more discussed below. Good agreement with measurements is obtained only in simulations using CBET and nonlocal transport. Simulations using flux-limited transport with or without CBET fail to consistently reproduce experiments.

The performance of implosions can be improved by mitigating CBET.<sup>15</sup> This paper considers three mitigation techniques: The first technique uses laser beam (or focal spot) diameter smaller than the target diameter. This can be very efficient in reducing CBET and increasing laser coupling; but on the downside, the narrow beams introduce beam-overlap nonuniformities, which can degrade the implosion performance. Experiments on OMEGA have been performed to investigate the optimum beam diameters by balancing CBET with the effects of nonuniformity in low-adiabat implosions. This is discussed below in details. The second technique employs multicolor laser light, which modifies resonance coupling between beams. Using, for example, two-color split, CBET can be reduced by a factor of 1/2 for the wavelength separation  $\Delta\lambda > 5\text{\AA}$  of the two wavelengths (for 351-nm light). The third technique uses targets with plastic ablators doped by high-Z elements (e.g., Ge).

This paper is organized as follows: Sec. II describes the simulation technique for modeling CBET (with details described in Appendices A, B, and C). Section III discusses CBET in OMEGA implosions, comparing simulations, and measurements. Section IV considers the three techniques for mitigating CBET: narrow beams, multicolor lasers, and Ge-doped plastic ablators. The conclusions are presented in Sec. V.

## II. MODELING CBET

The numerical algorithm for CBET considers pair-wise interactions of pump light rays (denoted with an index  $j$ ) with probe light rays (denoted with  $i$ ). All possible crossings in three-dimensions and corresponding energy transfers between the  $i$ -ray, which propagates along the path  $\ell$  in a target corona, and the  $j$ -rays, which come from different directions, are taken into account. The intensity of the probe light obeys the equation

$$\frac{dI_i}{d\ell} = \xi I_i \sum_j L_{ij}^{-1}, \quad (1)$$

where  $L_{ij}$  is the SBS spatial gain rate for the rays  $i$  and  $j$ , and  $\xi$  is a limiting parameter,<sup>15</sup>  $0 < \xi \leq 1$  (see Sec. III). The path  $\ell$  is calculated using Snell's law. The spatial gain  $L_{ij}$  is estimated in the strong damping limit,<sup>8</sup> which is well satisfied in direct-drive implosions,<sup>16</sup> and given in Appendices A and B for the fluid [Eq. (A2)] and kinetic [Eq. (B8)] models, respectively. A random polarization of the illuminating

beams in implosions is accounted in Eq. (1) by increasing  $L_{ij}$  by a factor of 2.

The algorithm uses a simplified assumption of spherical symmetry for both the implosion hydrodynamics and the laser illumination. Intensity profiles for laser beams can take an arbitrary shape (e.g., supergaussian  $n=4$  in the standard OMEGA setup). The beams are represented by a set of rays with different impact parameters  $a$  (typically 60), which range from 0 to  $1.4R_{\text{target}}$ , where  $R_{\text{target}}$  is the target radius. The ray trajectories are calculated using an inline two-dimensional (2-D) ray-tracing routine. The algorithm is incorporated into the laser-absorption package of the one-dimensional (1-D) hydrodynamic code *LILAC*,<sup>17</sup> allowing a self-consistent calculation of laser deposition with CBET.

Simulations of implosions with  $I \gtrsim 4 \times 10^{14} \text{ W/cm}^2$  show that the CBET model overpredicts scattered power, indicating that additional mechanisms that increase laser coupling may be present. This discrepancy is resolved by introducing a simple model for clamping the ion-acoustic waves.<sup>18</sup> The clamp model was incorporated in *LILAC* and is discussed in Appendix C.

## III. CBET IN OMEGA IMPLOSIONS

OMEGA implosions are used to validate the accuracy of the CBET model, comparing simulations with observables. Laser coupling is characterized by the time-dependent absorption fraction, inferred from scattered-light measurements, and scattered frequency spectra.<sup>14</sup> The hydrodynamic efficiency of simulated implosions can be constrained by bang-time (time of rising of the neutron rate)<sup>19</sup> and shell trajectory measurements (inferred from x-ray self-emission images of implosion targets).<sup>20</sup>

Simulations of implosions at  $I \gtrsim 4 \times 10^{14} \text{ W/cm}^2$  indicate that the CBET model overpredicts measured scattered light and, as a result, shows earlier bang times. The agreement with experiments can be improved by reducing CBET in simulations. This is accomplished by clamping ion-acoustic waves with the clamp parameter  $(\tilde{n}_e/n_e)_{\text{cl}}$  (Appendix C).<sup>18</sup> Simulations using a single clamp value show good agreement for implosions with different pulse shapes and intensities up to  $I \approx 6 \times 10^{14} \text{ W/cm}^2$  (for higher intensities, see below). Targets with different ablators, however, require different clamping. For example, it was found that  $(\tilde{n}_e/n_e)_{\text{cl}} \approx 0.1\%$  fits data for plastic and 10% fits data for glass ( $\text{SiO}_2$ ) ablators. In the previous study, CBET was reduced assuming  $\xi < 1$  in Eq. (1).<sup>15</sup> But this approach is less universal because it requires different  $\xi$  depending on the laser energy, pulse shapes, and targets.

The fluid and kinetic versions of the CBET model (Appendices A and B, respectively) were compared using implosions of plastic- and glass-shell targets. Little differences between the results of these versions were observed. The differences are typically smaller than deviations of simulations from measurements. The majority of simulation results discussed here is obtained using the fluid version, which is less expensive computationally.

Figure 3 compares measured and simulated scattered-light powers for a triple-picket, warm plastic-shell implosion

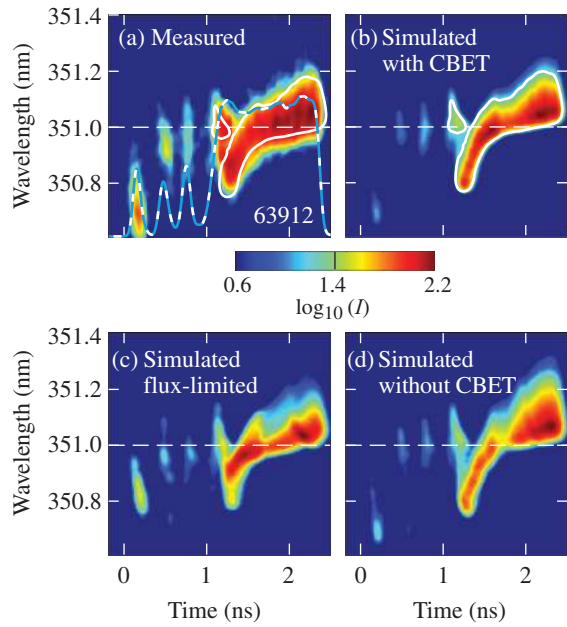


FIG. 4. Measured (a) and simulated scattered-light spectra for a warm plastic-shell implosion (OMEGA shot 63912). *LILAC* predictions using nonlocal transport and CBET are shown in (b), and simulations without CBET using flux-limited and nonlocal transports are shown in (c) and (d), respectively. The white contours in (a) indicate the shape of the simulated spectrum in (b). The incident light wavelength is presented by the dashed line.

with a main pulse intensity  $I = 4.5 \times 10^{14}$  W/cm<sup>2</sup> (OMEGA shot 63912).<sup>21</sup> The simulations employing the fluid CBET model with  $(\tilde{n}_e/n_e)_{cl} = 0.1\%$  (red long-dashed line) accurately reproduce the measured time-dependent scattered power (black thick solid line).

Figure 4 compares measured [Fig. 4(a)] and simulated with [Fig. 4(b)] and without CBET [Figs. 4(c) and 4(d)] scattered light spectra for the same implosion as in Fig. 3. The simulated spectra reproduce all basic features of the measured spectrum: time-dependent frequency shifts during pickets and an initial blue shift and later red shift of scattered light during the main pulse. The details and accuracy of reproduction of the measured spectrum depend, however, on the heat-transport model used and the presence of CBET.<sup>22</sup> The simulations using flux-limited transport [Fig. 4(c)] underestimate the blue shifts during the first picket and initial part of the main pulse indicating that the density and velocity distributions in the target corona are not accurately predicted. The simulations using nonlocal transport without CBET [Fig. 4(d)] overestimate the late-time red shift during the main pulse, and these with CBET [Fig. 4(b)] agree best with the measurements.

The predicted hydrodynamics efficiency of implosions can be verified using measured bang-time and ablation-front trajectories. Figure 5(a) shows the measured (black solid line) and simulated (blue short-dashed, green dashed-dotted, and red long-dashed lines) neutron-production histories for the same implosion as in Fig. 3. The experimental bang time for this implosion is about 2.95 ns. The simulations using nonlocal transport and CBET (red long-dashed line) show bang time coincided with the measured time within experimental uncertainty. The simulations without CBET, using both flux-limited (green dashed-dotted line) and nonlocal

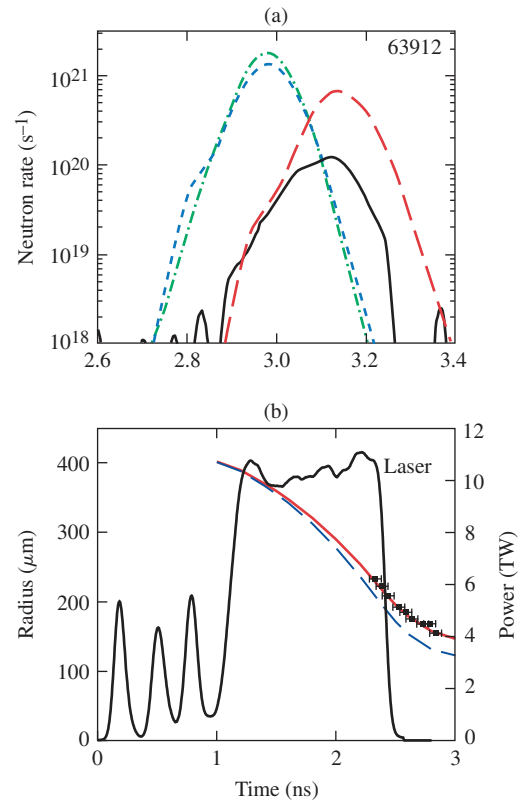


FIG. 5. (a) Neutron-production history measured (black solid line) and simulated with flux-limited transport (green dashed-dotted line), nonlocal transport (blue short-dashed line), and nonlocal transport and CBET (red long-dashed line). The measurements and simulations with CBET show good agreement between bang times, which are estimated as the rise time of the neutron rate. (b) Ablation-front trajectory inferred from x-ray framing camera images<sup>20</sup> (black dots), and the trajectories simulated using nonlocal transport with and without CBET (red solid and blue dashed lines, respectively). The simulations with CBET show good agreement with measurements.

transport (blue short-dashed line), predict bang times  $\sim 200$  ps earlier than measured. This is consistent with the higher predicted absorption (or underpredicted scattered-light power) shown in Fig. 3.

Figure 5(b) shows the measured (squares) and simulated ablation-front trajectories, where the simulations use nonlocal transport with and without CBET (red solid and blue dashed lines, respectively). The simulated trajectories were inferred from x-ray images obtained by post processing the *LILAC* simulations using the collisional-radiative code *SPEC3D*.<sup>23</sup> The trajectory simulated using CBET agrees well with the measured trajectory. The simulations without CBET predict a faster implosion.

Neutron yield is perhaps the most important characteristic of implosions; however, it cannot be directly used to validate the CBET model. This is because the neutron-production rate strongly depends on temperature and density distributions inside the hot spot.<sup>1</sup> Low-adiabat, warm implosions on OMEGA typically produce yields that are 20%–25% of *LILAC*-simulated yields. This about factor-of-4 yield reduction is unlikely due to inaccuracies in the CBET model but more likely due to asymmetry of implosions. Relative yields, however, are used to study the mitigation of CBET in Sec. IV A.

The CBET model was validated using different targets, laser energies, and pulse shapes and shows good and consistent agreement with measurements (see other examples in Ref. 15) up to intensities  $I \approx 6 \times 10^{14} \text{ W/cm}^2$ . At higher intensities of  $I \sim 10^{15} \text{ W/cm}^2$ , the CBET model predicts more scattered light than measured, indicating the presence of an additional absorption mechanism that increases laser coupling. Possible candidates for this mechanism include two-plasmon-decay instability (TPD),<sup>24</sup> which converts incident light into plasma waves with a subsequent dissipation of these waves,<sup>25</sup> and saturation of SBS in intense laser speckles.<sup>26</sup>

Glass-shell implosions were not studied as thoroughly as the plastic-shell implosions discussed above. Only a few implosions were analyzed and were in good agreement with simulations using an appropriate clamp parameter. Figure 6 presents an example of a glass-shell implosion that used an 860- $\mu\text{m}$ -diameter, 20- $\mu\text{m}$ -thick glass shell filled with 20 atm of  $D_2$ -gas. A shaped pulse [the thin black line in Fig. 6(a)] with 26 kJ of energy used to provide an on-target intensity of  $I \approx 10^{15} \text{ W/cm}^2$ . The best agreement between measured and predicted scattered-light and neutron-production histories [see Figs. 6(a) and 6(b), respectively] was obtained using simulations with nonlocal transport and CBET, in which  $(\tilde{n}/n_e)_{\text{cl}} = 10\%$  (compare thick black solid and red long-dashed lines). Simulations without CBET using flux-limited and nonlocal transports [the green dashed-dotted and blue

short-dashed lines in Figs. 6(a) and 6(b)] show significant disagreement with measurements.

#### IV. MITIGATION OF CBET

CBET significantly reduces laser coupling in direct-drive implosions. While the laser absorption in a typical OMEGA implosion is reduced by  $\sim 10\%$ , the implosion hydrodynamic efficiency is reduced by  $\sim 20\%$ . This can be attributed to the laser deposition area moving outward from the critical surface when CBET is present.<sup>15</sup> Laser coupling can be partially or, in some cases, completely recovered by employing different mitigation techniques for CBET. Three such techniques are considered below. One technique uses narrow laser beams and is extensively tested in OMEGA experiments and simulations. Other two techniques use multicolor lasers and high-Z dopant ablaters.

##### A. Narrow beams

The idea of using narrow beams to mitigate CBET is illustrated in Fig. 2 that shows a ray geometry with the most efficient energy transfer. The standard OMEGA implosions use targets with about the same radius as the beam radius,  $R_{\text{target}} \approx R_{\text{beam}}$ . By narrowing the beams, one can eliminate edge-beam rays that seed CBET. Figure 7 quantitatively illustrates the contribution of different parts of beams to CBET. This figure shows the simulated distributions of energy  $E$  transferred to (when  $dE/da > 0$ ) or from (when  $dE/da < 0$ ) light rays with an impact parameter  $a$ . The outgoing rays (blue short-dashed line) always gain energy, and the gain reaches the maximum for rays with  $a/R_{\text{target}}$  from  $\sim 0.7$  to 1.1. The incoming rays (green dashed-dotted line) mostly lose energy, transferring it to outgoing rays. This loss takes place for  $a/R_{\text{target}}$  from 0 to  $\sim 0.9$  and is peaked at  $a/R_{\text{target}} \sim 0.5$ . The incoming rays with  $a/R_{\text{target}} \gtrsim 0.9$  gain some energy, but this gain is not significant. The rays with  $0.5 \lesssim a/R_{\text{target}} \lesssim 0.9$  lose energy as they travel toward the target and gain it on the way out. The cumulative effect of

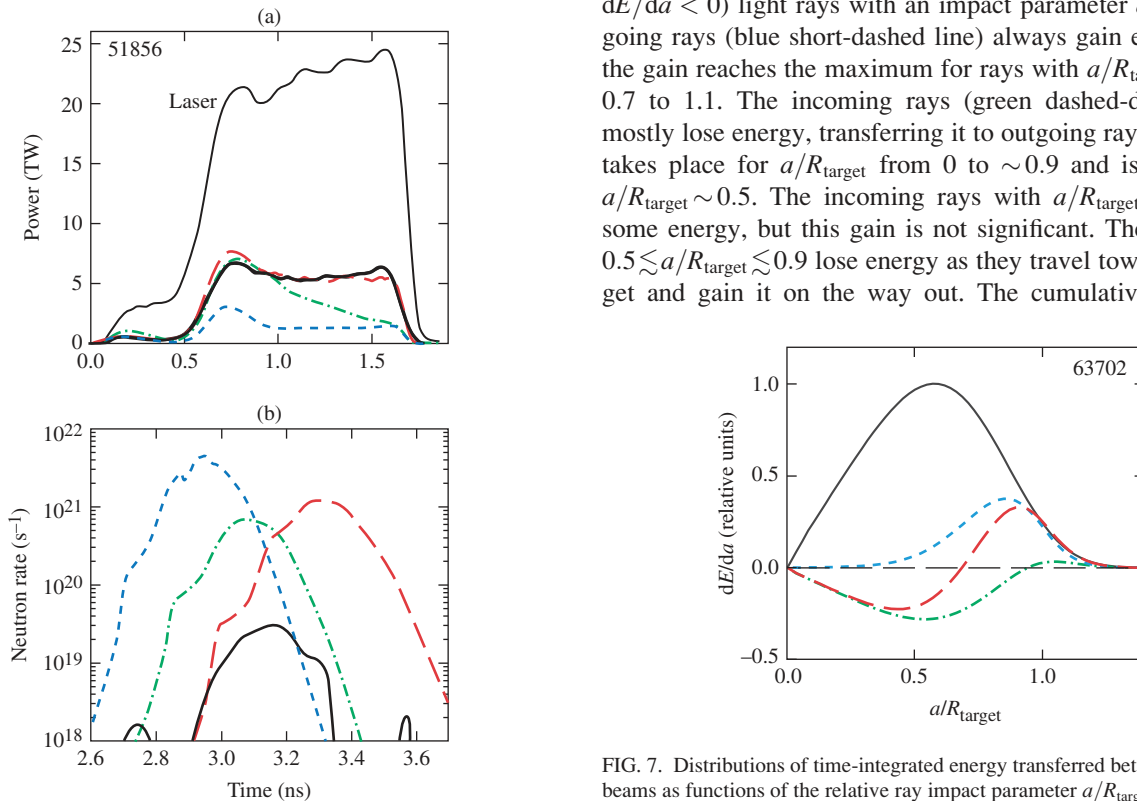


FIG. 6. (a) Reflected light power history in a glass-shell implosion (OMEGA shot 51856). For notations, see Fig. 3. (b) Neutron-production history measured and simulated. For notations, see Fig. 5(a). Note good agreement of the measured scattered light and bang time in (a) and (b) with the simulations using CBET and poor agreement with the simulations not using CBET.

FIG. 7. Distributions of time-integrated energy transferred between crossing beams as functions of the relative ray impact parameter  $a/R_{\text{target}}$  in a plastic-shell implosion (OMEGA shot 63702). Distribution of the incident energy is shown by the black solid line. Distribution of the transferred energy for the incoming trajectories is shown by the green dashed-dotted line, for the outgoing trajectories by the blue short-dashed line, and for whole trajectories (including the incoming and outgoing parts) by the red long-dashed line. The negative  $dE/da$  corresponds to energy losses, and the positive one to energy gains.

CBET for the whole ray trajectory (including the incoming and outgoing parts) is shown by the red long-dashed line in Fig. 7. The rays with  $a/R_{\text{target}} < 0.7$  lose energy, and the rays with  $a/R_{\text{target}} > 0.7$  gain energy. This suggests that by eliminating rays with  $a/R_{\text{target}} > 0.7$ , one can completely suppress CBET.

Figure 8 shows simulation results for implosions at the same conditions [similar to the one shown in Fig. 1(c)] except using different beam radii  $R_{\text{beam}}$ , which are defined to incirculate 95% energy. The beam radius is changed by defocusing beams with an assumed profile  $I(r) \sim \exp[-(r/r_0)^{2.1}]$ , where  $r_0 = 135 \mu\text{m}$ . The ratio  $R_{\text{beam}}/R_{\text{target}}$  is varied from 0.5 to 1.1. The simulations including CBET (solid line) show a decrease in scattered energy when  $R_{\text{beam}}/R_{\text{target}}$  is decreased. The scattered energy in the simulations without CBET (long-dashed line) is reduced as well. This is because smaller beams provide illumination of the target surface by more-normal incident light. Such light penetrates deeper into the target corona and is absorbed more efficiently. Thus, the benefits of using smaller beams include two aspects: reducing CBET and increasing absorption as a result of more-normal incident light.

The smaller beams can have a negative effect on implosion performance because of increasing beam-overlap nonuniformities. 2-D hydrodynamic simulations using the code *DRACO* (Ref. 27) predict nearly symmetric implosions and small reduction in neutron yield for  $R_{\text{beam}}/R_{\text{target}}$  from  $\sim 1$  to 0.8 [see Figs. 9(a) and 9(b)]. Simulations assuming  $R_{\text{beam}}/R_{\text{target}} \lesssim 0.7$  show significantly distorted targets at maximum compression and reduced neutron yields [by a factor of 2 or more, see Fig. 9(c)]. These 2-D results agree with the simple calculations of deposition nonuniformities presented in Fig. 8 (red short-dashed line). The calculations predict a significant increase in targets nonuniformities in the range of  $R_{\text{beam}}/R_{\text{target}}$  from 0.7 to 0.8. Therefore, these results suggest an optimum  $R_{\text{beam}}/R_{\text{target}} \sim 0.8$  that balances the reduction of CBET and increase of beam-overlap nonuniformities.

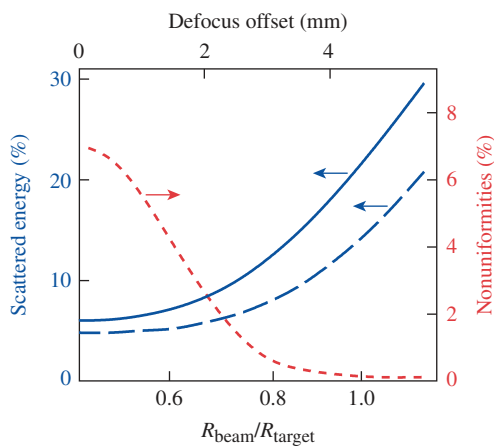


FIG. 8. Predicted scattered energy and deposition nonuniformities (rms) as functions of  $R_{\text{beam}}/R_{\text{target}}$  in plastic-shell implosions. The scattered energy is normalized to the incident energy. The simulated energies with and without CBET are shown by the blue solid and long-dashed lines, respectively. The deposition nonuniformities (red short-dashed line) are calculated using the OMEGA beam-port geometry and time averaging over the whole laser pulse.

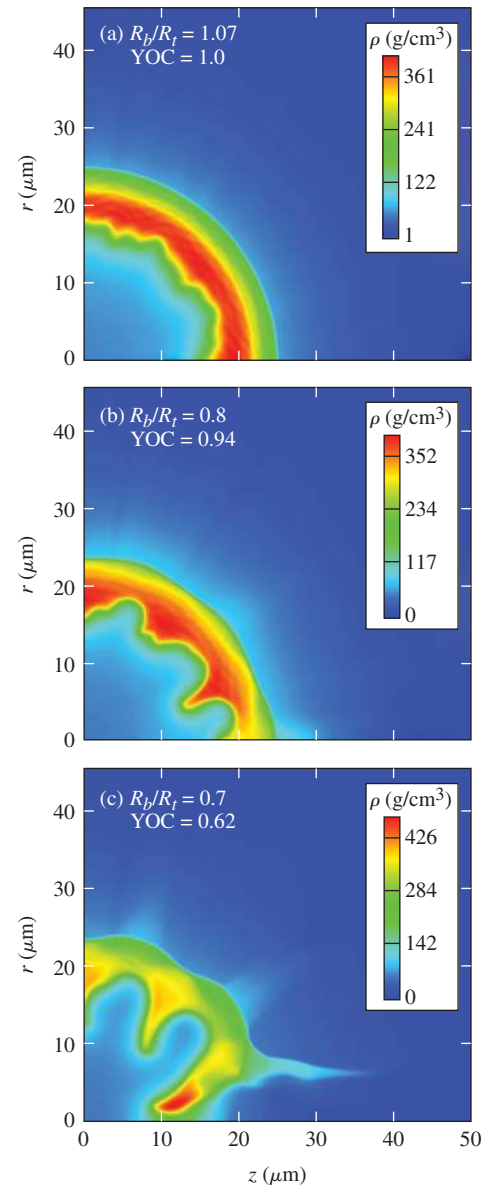


FIG. 9. Density distributions at maximum compression from 2-D hydrodynamics simulations of implosion targets illuminated by different-sized laser beams: (a)  $R_{\text{beam}}/R_{\text{target}} = 1.07$ , (b) 0.8, and (c) 0.7. Beam-overlap nonuniformities in the case of small  $R_{\text{beam}}/R_{\text{target}}$  result in asymmetric implosions and degradation of neutron yield. Each simulation shows yield over clean (YOCC, which is 2-D yield normalized to 1-D yield).

Two sets of implosion experiments on OMEGA were performed to investigate the effects of narrow beams. These experiments use triple-picket pulses with a peak overlap intensity  $I \approx 4.5 \times 10^{14} \text{ W/cm}^2$  that drive targets with an adiabat (the ratio of the pressure in an imploding shell to the Fermi-degenerated pressure<sup>1</sup>)  $\alpha \approx 4$ . The primary goal of the first set of experiments is to demonstrate enhanced laser coupling in implosions with narrow-beam illumination.<sup>28</sup> The experiments use fixed-diameter (860- $\mu\text{m}$ ) nominal OMEGA targets and variable-diameter beams. The beam diameters are varied by defocusing beams obtained using small distributed phase plates (DPPs).<sup>29</sup> Figure 10 shows the measured beam profiles for different defocus offsets corresponding to different  $R_{\text{beam}}/R_{\text{target}}$ .

The experiments with variable beams use a range of  $R_{\text{beam}}/R_{\text{target}}$  from 0.5 to 1.09. Figure 11 compares measured

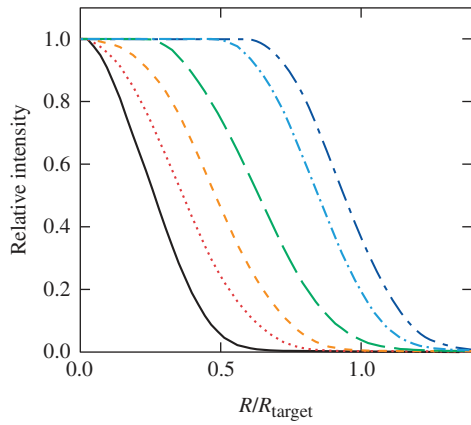


FIG. 10. Measured profiles of beams with small DPPs at different defocus offsets. The beam profile at best focus is shown by the solid line, and wider beams have increasing defocus offsets. These profiles correspond to  $R_{\text{beam}}/R_{\text{target}} = 0.5, 0.65, 0.74, 0.88, 1.0,$  and  $1.09$  (from narrow to wide, respectively).

and simulated scattered-light spectra for wide and narrow beams ( $R_{\text{beam}}/R_{\text{target}} = 1.0$  and  $0.5$ , respectively). Note the good agreement between the simulated and measured spectra. The implosion with narrow beams and reduced CBET shows the presence of the red-shifted part of the spectrum, which corresponds to light that deeply penetrates inside the target corona. The implosions with wide beams ( $R_{\text{beam}}/R_{\text{target}} = 1.0$ ) do not show such red-shifted parts, indicating that deeply penetrated light has been scattered.

Figure 12 shows the scattered-light fractions in implosions with different  $R_{\text{beam}}/R_{\text{target}}$ . The measured fractions (red solid circles with error bars) are reduced in implosions with narrower beams, in agreement with simulations including CBET (blue triangles and solid line). The reduction of

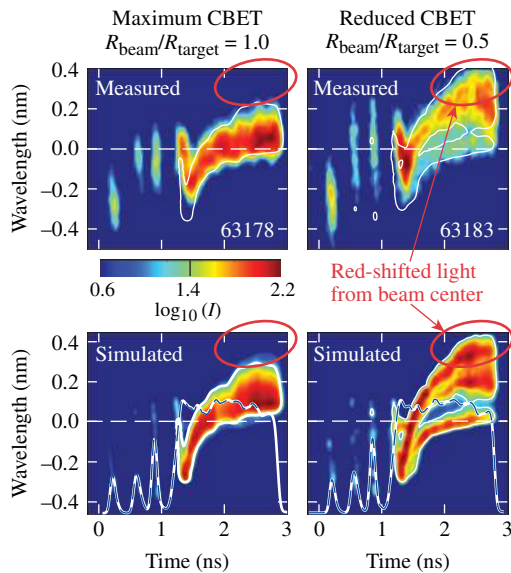


FIG. 11. Measured and simulated scattered-light spectra for plastic-shell implosions using wide and narrow laser beams ( $R_{\text{beam}}/R_{\text{target}} = 1.0$  and  $0.5$ , respectively). The implosion with narrow beams recovers the red-shifted part of the spectrum (indicated by the red ovals), which corresponds to rays that deeply penetrate into the target corona. These rays are not present in the implosion with wide beams ( $R_{\text{beam}}/R_{\text{target}} = 1.0$ ) because of CBET. Note good agreement between measured and simulated spectra.

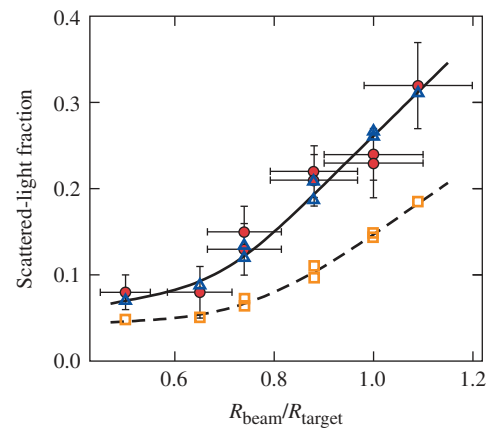


FIG. 12. Scattered-light fractions in implosion experiments using variable-diameter beams. Measurements corresponding to implosions with different  $R_{\text{beam}}/R_{\text{target}}$  are shown by the red solid circles with error bars. Simulation results with and without CBET are shown by the blue open triangles and orange open squares, and approximated by the solid and dashed lines, respectively. The measured fractions are in good agreement with the simulated ones including CBET.

scattered light and corresponding increase of absorption result in earlier bang times in implosions with narrow beams. Figure 13 summarizes the bang-time measurements and shows good agreement between the measurements (red solid circles) and simulations with CBET (blue triangles).

The earlier bang times correspond to higher velocity implosions in agreement with the results of the ablation-front trajectory measurements. Figure 14(a) shows two examples of trajectories both measured (dots) and simulated with CBET (lines), for  $R_{\text{beam}}/R_{\text{target}} = 1.0$  and  $0.75$ . The targets illuminated with smaller beams clearly demonstrate higher velocity. Figure 14(b) compares the implosion velocities inferred from the measured trajectories (squares) and those simulated with and without CBET (red solid triangles and blue diamonds, respectively). Higher implosion velocities are achieved with smaller beams in both measurements and simulations, and the simulations with CBET show good agreement with the measured data.

The described experiments, however, cannot be used to demonstrate improvements in neutron yield because of

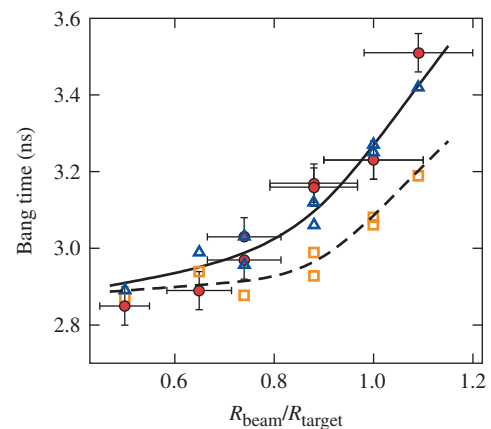


FIG. 13. Bang times in implosion experiments using variable-diameter beams. For notations, see Fig. 12. The measured bang times are in good agreement with the simulated ones including CBET.



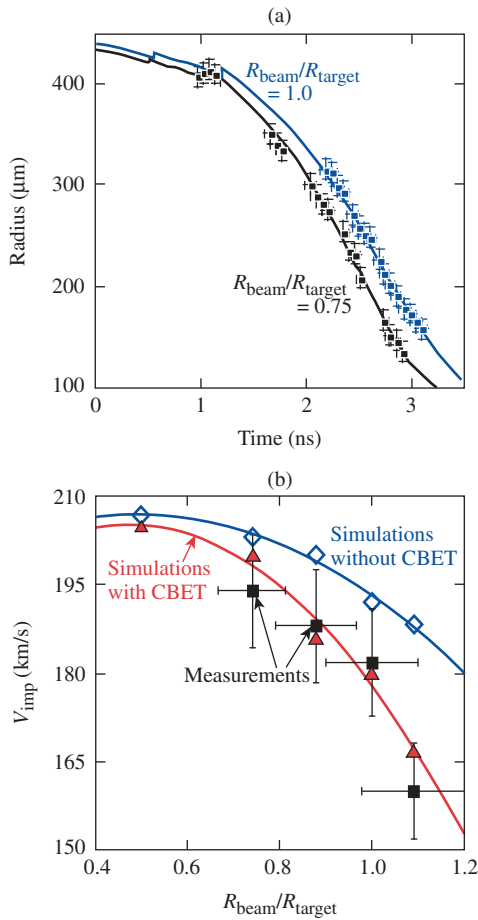


FIG. 14. (a) Ablation-front trajectories inferred from x-ray framing-camera images (dots) and simulated (lines) in implosions with wide and narrow beams ( $R_{\text{beam}}/R_{\text{target}} = 1.0$  and  $0.75$ , respectively). (b) Measured (black square dots) and simulated with (red line and triangles) and without CBET (blue line and diamonds) implosion velocities as functions of  $R_{\text{beam}}/R_{\text{target}}$ . Higher implosion velocities are achieved with smaller beams in both measurements and simulations.

significant level of single-beam nonuniformity (imprint) in the beams with small DPPs. As a result, measured neutron yields are reduced by a factor of 5–10 with respect to the yields in similar implosions but illuminated with best uniformity. To address the issue of yield improvement, additional experiments employing uniform beams with standard OMEGA SG4 DPPs, polarization smoothing (PS),<sup>30</sup> and smoothing by spectral dispersion (SSD)<sup>31</sup> were performed. The SG4 DPPs with PS and SSD are optimized for the on-target uniformity in the case of 860- $\mu\text{m}$ -diameter targets. These experiments vary  $R_{\text{beam}}/R_{\text{target}}$  by changing the target size. Three target diameters were used, 860, 950, and 1000  $\mu\text{m}$ , which correspond to  $R_{\text{beam}}/R_{\text{target}} = 0.97$ , 0.88, and 0.83, respectively. This range of  $R_{\text{beam}}/R_{\text{target}}$  was narrower than that used in the previous set of experiments, but covers the important region around  $R_{\text{beam}}/R_{\text{target}} \sim 0.8$ , where significant changes in neutron yield are expected because of beam-overlap nonuniformities. To reduce the effects of small-scale single-beam imprinting, the implosions were designed to be robust to Rayleigh–Taylor instability,<sup>32</sup> having relatively low in-flight aspect ratio (IFAR)  $\approx 30$ ,<sup>1</sup> which was constant for all targets.

Figure 15(a) shows measured neutron yields that were normalized to simulations including CBET (circles) as a function of  $R_{\text{beam}}/R_{\text{target}}$ . If all nonuniformity sources are kept constant for different  $R_{\text{beam}}/R_{\text{target}}$ , then expected measured yields normalized to predicted yields should be independent of  $R_{\text{beam}}/R_{\text{target}}$ . This is shown in Fig. 15(a) by the dashed line. The data follow this line down to  $R_{\text{beam}}/R_{\text{target}} \approx 0.86$ . For smaller  $R_{\text{beam}}/R_{\text{target}}$ , the relative yields drop due to enhanced beam-overlap nonuniformity. Figure 15(b) demonstrates the benefit of using narrow beams, showing the same measurements as in Fig. 15(a) but normalized to simulations without CBET and assuming  $R_{\text{beam}}/R_{\text{target}} = 1$ . Such a normalization uses “clean” yields without both beneficial effects of narrow beams: reduced CBET and more-normal light illumination. The relative yields in Fig. 15(b) show an increase by a factor of  $\sim 1.5$  for smaller beams with the maximum yield at  $R_{\text{beam}}/R_{\text{target}} \approx 0.88$ . Further reduction of  $R_{\text{beam}}/R_{\text{target}}$  results in a reduction in yields, indicating that beam-overlap nonuniformities dominate the target performance. These data demonstrate the beneficial effects of reducing  $R_{\text{beam}}/R_{\text{target}}$  from  $\sim 1$  down to  $\approx 0.85$ .

## B. Multi-color lasers

The efficiency of CBET is determined by the SBS gain, which is resonant and sensitive to a wavelength separation

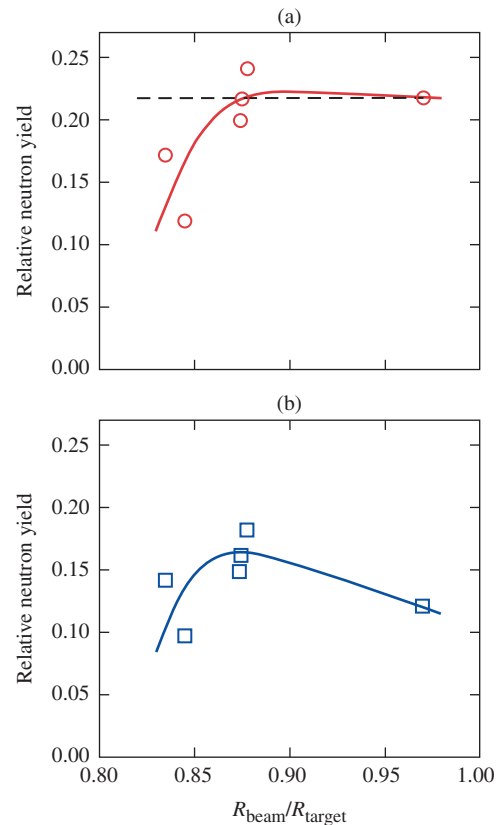


FIG. 15. Relative neutron yields in experiments using uniform beams and variable-diameter targets. (a) Measured yields normalized to simulations with CBET (circles). (b) The same yields as in (a) but normalized to simulations without CBET and having  $R_{\text{beam}}/R_{\text{target}} = 1$  (squares). The solid lines in (a) and (b) approximate the data points. The dashed line in (a) shows an expected constant relative yield in the case of similar uniformity. The drop of relative yields at  $R_{\text{beam}}/R_{\text{target}} < 0.86$  is due to beam-overlap nonuniformities.

$\Delta\lambda$  between interacting beams [see Eqs. (A2) and (B8) in Appendices A and B]. Changing the wavelengths of beams affects the SBS gain and, therefore, increases or decreases CBET. Benefits of a wavelength separation technique were recently demonstrated in indirect-drive implosions on the NIF.<sup>33</sup> The applied  $\Delta\lambda$  in these implosions is relatively small (up to  $\sim 3\text{\AA}$  in UV light). Mitigation of CBET in direct-drive implosions requires a larger  $\Delta\lambda$  among beams to eliminate the coupling resonances.<sup>15</sup>

To illustrate the CBET mitigation effect in direct-drive experiments, consider the simplest case of a laser system operating on two subsets of lasers with wavelengths separated by  $\Delta\lambda$ . These wavelengths can be distributed among different beams, or each beam can include both wavelengths (e.g., as a uniform mix, or one wavelength is at the center and other is at the edge of a beam). For a large separation,

$$\Delta\lambda \gg \lambda_L(c_a/c) \sim 5\text{\AA}, \quad (2)$$

one subset does not see the presence of the other and there is no interaction between them [e.g., see Eq. (A2)]. Here,  $c_a = \sqrt{(ZT_e + 3T_i)/M_i}$  is the ion-acoustic sound speed,  $Z$  is the ionization,  $M_i$  is the ion mass, and  $T_e$  and  $T_i$  are the electron and ion temperatures, respectively. In this case of large  $\Delta\lambda$ , CBET occurs only within each subset and, therefore, the total CBET is reduced by 1/2 with respect to the case of  $\Delta\lambda = 0$ . [This reduction is equivalent to assuming  $\xi = 1/2$  in Eq. (1).] Figure 16 shows simulated absorption fractions (solid line) for a plastic-shell implosion driven by two-color illumination as a function of  $\Delta\lambda$ . The absorption fraction changes very little for  $\Delta\lambda < 3\text{\AA}$  and increases significantly (by up to 10%) for  $\Delta\lambda > 5\text{\AA}$ . The dashed line in Fig. 16 shows the asymptotic limit of 1/2 CBET. In general, an  $N$ -color separation can result in the asymptotic reduction of CBET by a factor of  $1/N$ .

As a practical application of laser drive using two or more colors distributed among different beams, a uniform spatial mix of these beams is suggested. More beams will provide a better mixing uniformity, and using more colors is more beneficial in reducing CBET.

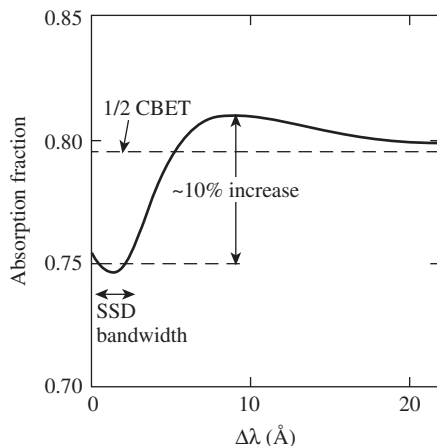


FIG. 16. Simulated absorption fraction (solid line) as a function of the wavelength separation  $\Delta\lambda$  in a plastic-shell implosion using two-color light. The upper dashed line corresponds to 50%-reduced CBET using one-color light.

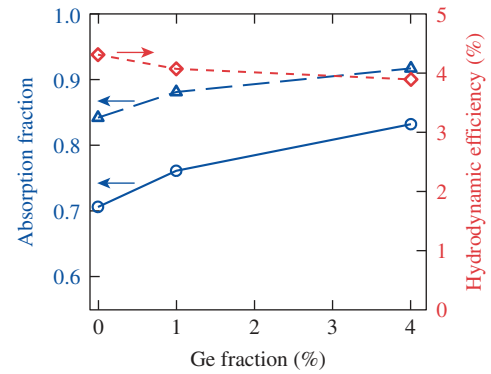


FIG. 17. Simulated absorption fractions with (blue solid line and circles) and without (blue long-dashed line and triangles) CBET for imploded plastic shells with different fractions of doped Ge. The effect of CBET is reduced in implosions with a higher-Ge dopant. Hydrodynamic efficiency in implosions with CBET (red short-dashed line and diamonds) is decreased with increasing-Ge dopant.

The results discussed in this section neglect the effects of TPD instability and laser speckles. The presence of speckles and anomalous absorption due to TPD can significantly modify the results shown in Fig. 16 that were obtained using a simple linear theory and the planar wave approximation [Eq. (1)]. Implosion experiments on OMEGA suggest that both these mechanisms, TPD and speckles, are not important at intensities  $I \lesssim 6 \times 10^{14} \text{ W/cm}^2$  (Sec. III). One can expect that the multicolor technique can work in implosions within this range of intensities, and more theoretical study is required to accurately predict laser coupling at higher intensities.

### C. High-Z dopants

The dependence of CBET on plasma ion charge  $Z$  is complex (see Appendices A and B). Ion charge also affects other aspects of implosion physics, in particular, heat transport, and hydrodynamics.

Figure 17 presents simulation results for implosion plastic shells with the varied dopant concentrations of Ge: 0%, 1%, and 4%. The absorption fraction grows with increased Ge concentration in simulations both including (circles) and not including (triangles) CBETs. The simulations including CBET show an  $\sim 6\%$  larger increase in absorption for 4%-Ge doping. These indicate a reduction of CBET in implosions with doped ablaters, which is mainly caused by increased coronal electron temperature in these implosions. On other hand, because of less-effective heat transport in a higher- $Z$  coronal plasma, the hydrodynamic efficiency of these implosions is reduced. The simulations show that 4%-Ge-dopant reduces the hydrodynamic efficiency by  $\sim 5\%$  (see red diamonds in Fig. 17), reducing the overall benefit of using high- $Z$  dopants in direct-drive implosions.

## V. CONCLUSIONS

CBET can significantly reduce the performance of direct-drive ICF implosions. It is responsible for about 10% reduction of laser absorption and about 20% reduction of hydrodynamic efficiency in implosion experiments on OMEGA. CBET is observed in time-resolved, scattered-light

spectra as a suppression of red-shifted light during the main laser drive. This light is present in simulations without CBET indicating that CBET mostly scatters the center-beam incoming light, which otherwise would penetrate to higher-density corona regions, where it is reflected with the maximum red shift.

Two models of CBET have been developed and implemented into the laser-absorption package of the 1-D hydrodynamic code *LILAC*: a fluid model (Appendix A) and a kinetic model (Appendix B), assuming spherically symmetric laser illumination of implosion targets. Both models were extensively tested using different OMEGA implosions with varied laser energies, pulse shapes, and target structure and composition. These demonstrated good agreement between model predictions and observables, which include scattered-light spectra and power, bang times, shell trajectories, and neutron yields (Sec. III). The fluid and kinetic models show quite similar results between each other.

The performance of direct-drive targets can be improved by mitigating CBET. This paper considered three mitigation techniques: using narrow beams, using multicolor lasers, and high- $Z$  doped ablaters. The first technique is efficient in improving laser coupling. The implosion experiments on OMEGA show a significant decrease of scattered-light power, earlier bang times, and an increase in implosion velocity (see Figs. 12–14) when reducing the beam radius. The small beams introduce more beam-overlap nonuniformities that reduce implosion performance by decreasing neutron yields. The experiments on OMEGA suggest an optimum  $R_{\text{beam}}/R_{\text{target}} \sim 0.85$  that maximizes the performance by balancing CBET with the effects of beam-overlap nonuniformities (see Fig. 15).

Simulations suggest that using multicolor lasers can be another efficient technique to mitigate CBET. By splitting light on  $N$  separate colors, CBET can be reduced by a factor of  $\sim 1/N$ . This technique requires, however, relatively large wavelength separations  $\Delta\lambda$  [Eq. (2)], which probably cannot be achieved on the OMEGA and NIF lasers. To utilize the multicolor split technique, future direct-drive laser systems should be designed to use subsets of lasers operating on different wavelengths. Such systems can benefit from using the narrow-beam technique discussed above and using many separate beams to reduce beam-overlap nonuniformity.

Test simulations of implosion plastic shells doped with high- $Z$  elements reveal no advantages to using this technique. Unless the simulations show a relative reduction in CBET and improvement in laser coupling in the case of Ge-doped targets, the overall implosion performance suffers because of the reduction of heat transport in a higher- $Z$  coronal plasma (see Fig. 17).

## ACKNOWLEDGMENTS

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## APPENDIX A: FLUID EQUATIONS

The fluid approach for the CBET model is based on the electron-density equation, the equation of motion for ions, and the wave equation for laser light.<sup>8</sup> The steady-state interaction of two s-polarized light waves and an ion-acoustic wave is considered in the strong damping limit. Details of derivation of the equation for the probe-light intensity  $I_{\text{probe}}$  is given in Ref. 9, and this equation can be written as

$$\frac{dI_{\text{probe}}}{d\ell} = \frac{I_{\text{probe}}}{L}, \quad (\text{A1})$$

where  $\ell$  is the probe-light path,

$$L^{-1} = \frac{\pi}{\lambda_L} \frac{n_e/n_{\text{cr}}}{\sqrt{1 - n_e/n_{\text{cr}}}} \frac{1}{[\tilde{\nu}_a^2 \eta^2 + (1 - \eta^2)^2]^{1/2}} \left( \frac{I_{\text{pump}}}{I_{\text{probe}}} \right)^{1/2} \left| \frac{\tilde{n}_e}{n_e} \right| \quad (\text{A2})$$

is the SBS gain rate,

$$\left| \frac{\tilde{n}_e}{n_e} \right| = \frac{e^2 \lambda_L^2}{\pi m_e^2 c^3} \frac{Z}{c_a^2} \left( \frac{m_e}{M_i} \right) \frac{(I_{\text{probe}} I_{\text{pump}})^{1/2}}{[\tilde{\nu}_a^2 \eta^2 + (1 - \eta^2)^2]^{1/2}} \quad (\text{A3})$$

is the relative amplitude of electron-density perturbations in the ion-acoustic wave, and  $I_{\text{pump}}$  is the pump-light intensity. In Eqs. (A2) and (A3),  $\tilde{\nu}_a = \nu_a/k_a c_a$  is the dimensionless damping of ion-acoustic waves.<sup>34</sup> The variable  $\eta$  includes the dependency on geometry and frequency of the interacting waves,

$$\eta = \frac{(\mathbf{k}_a \cdot \mathbf{u})}{k_a c_a} - \frac{\omega_a}{k_a c_a}, \quad (\text{A4})$$

where  $\mathbf{u}$  is the flow velocity and  $\omega_a$  and  $\mathbf{k}_a$  are the ion-acoustic wave frequency and wave vector, respectively. The interacting waves satisfy the following three-wave matching conditions:

$$\omega_a = \omega_{\text{probe}} - \omega_{\text{pump}} \quad (\text{A5})$$

and

$$\mathbf{k}_a = \mathbf{k}_{\text{probe}} - \mathbf{k}_{\text{pump}}. \quad (\text{A6})$$

The frequency changes in probe and pump light are calculated considering the plasma expansion and Doppler effects.<sup>35</sup> More details of implementation of Eq. (A1) into *LILAC* can be found in Ref. 15.

## APPENDIX B: KINETIC EQUATIONS

The electron-density perturbation  $\tilde{n}_e$  in an ion-acoustic wave is calculated using the linearized Vlasov equations for electrons and ions and the Poisson equation for the self-consistent electrostatic potential. One gets<sup>36</sup>

$$\tilde{n}_e = \frac{k_a^2 \phi_p}{4\pi e} \frac{\chi_e (1 + \sum_i \chi_i)}{1 + \chi_e + \sum_i \chi_i}, \quad (\text{B1})$$

where the summation is taken over all ion species,  $\phi_p$  is the beat ponderomotive potential of interacting light waves, and  $\chi_e$  and  $\chi_i$  are the electron and ion linear susceptibilities, respectively, which can be written as follows:

$$\chi_e \approx \omega_{pe}^2 / k_a^2 v_{Te}^2, \quad (\text{B2})$$

$$\chi_i = \frac{\omega_{pi}^2}{k_a^2 v_{Ti}^2} \left( 1 + \frac{x}{\sqrt{\pi}} \int_{-\infty}^{\infty} \frac{e^{-z^2}}{z-x} dz \right), \quad (\text{B3})$$

and

$$x = \frac{\omega_a + i\nu_{ie} - (\mathbf{k}_a \cdot \mathbf{u})}{\sqrt{2} k_a v_{Ti}}. \quad (\text{B4})$$

In the above equations,  $v_{Te} = (T_e/m_e)^{1/2}$  and  $v_{Ti} = (T_i/M_i)^{1/2}$  are the electron and ion thermal velocities, respectively,  $\nu_{ie}$  is the ion–electron collisional frequency, and  $\omega_{pe} = (4\pi e^2 n_e/m_e)^{1/2}$  and  $\omega_{pi} = (4\pi e^2 Z n_e/M_i)^{1/2}$  are the electron and ion plasma frequencies, respectively.

The equation for light waves is

$$\frac{\partial^2 \mathbf{A}}{\partial t^2} - c^2 \Delta \mathbf{A} + \omega_{pe}^2 \left( 1 + \frac{\tilde{n}_e}{n_e} \right) \mathbf{A} = 0. \quad (\text{B5})$$

Assuming that the probe and pump waves are s-polarized, the corresponding component of the vector potential  $\mathbf{A}$  can be expressed as

$$A(\mathbf{r}, t) = \frac{1}{2} [A_{\text{probe}} \exp(-i\omega_{\text{probe}} t + i\mathbf{k}_{\text{probe}} \cdot \mathbf{r}) + A_{\text{pump}} \exp(-i\omega_{\text{pump}} t + i\mathbf{k}_{\text{pump}} \cdot \mathbf{r}) + c.c.]. \quad (\text{B6})$$

Then the potential  $\phi_p$  takes the form

$$\phi_p = -\frac{e}{2m_e c^2} A_{\text{probe}} A_{\text{pump}}^*. \quad (\text{B7})$$

Substituting Eq. (B1) into Eq. (B5) and using Eqs. (B6) and (B7) and the definition  $A^2 = 8\pi c I / \omega_L^2$ , where  $\omega_L$  is the laser frequency, one obtains the equation for the probe light-intensity  $I_{\text{probe}}$ , similar in form to Eq. (A1), in which

$$L^{-1} = \frac{\pi}{\lambda_L} \frac{n_e/n_{cr}}{\sqrt{1 - n_e/n_{cr}}} \frac{\text{Im}(B)}{|B|} \left( \frac{I_{\text{pump}}}{I_{\text{probe}}} \right)^{1/2} \left| \frac{\tilde{n}_e}{n_e} \right|, \quad (\text{B8})$$

$$\left| \frac{\tilde{n}_e}{n_e} \right| = \frac{e^2 \lambda_L^2 k_a^2 (I_{\text{probe}} I_{\text{pump}})^{1/2}}{\pi m_e^3 c^3 \omega_{pe}^2 |B|}, \quad (\text{B9})$$

and

$$B = \frac{1 + \chi_e + \sum_i \chi_i}{\chi_e (1 + \chi_i)}. \quad (\text{B10})$$

The interacting ion-acoustic and light waves satisfy the matching conditions given by Eqs. (A5) and (A6). Equations (B8) and (B9) substitute the fluid approach equations [Eqs. (A2) and (A3)] in the numerical procedure when the kinetic option is chosen.

## APPENDIX C: THE CLAMP MODEL

The amplitude of ion-acoustic waves can experience a nonlinear saturation, depending on the laser intensities and ion composition of a plasma. This saturation can reduce an energy transfer predicted by the CBET model. A simple model for clamping of ion-acoustic waves was proposed<sup>18</sup> that limits the amplitude of electron-density perturbations  $|\tilde{n}_e/n_e|$  defined by Eqs. (A3) and (B9) for the fluid and kinetic models, respectively. Specifically, the corresponding values of  $|\tilde{n}_e/n_e|$  in Eqs. (A2) and (B8) are substituted by

$$\left\langle \frac{\tilde{n}_e}{n_e} \right\rangle = \min \left[ \left| \frac{\tilde{n}_e}{n_e} \right|, \left( \frac{\tilde{n}_e}{n_e} \right)_{\text{cl}} \right]. \quad (\text{C1})$$

The clamping parameter  $(\tilde{n}_e/n_e)_{\text{cl}}$  is determined by comparing simulations with experiments.

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