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Meteorological and hydrological drought monitoring using several drought indices

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Abstract

With respect to the necessity of comprehensive studies on drought and also high damages that caused by drought, this research studied the meteorological and hydrological droughts. In this study, Lighvan, Navroud and Seqez basins with different climates were selected. We used monthly data of stream flow, precipitation and evaporation from 1992 to 2016 for the study of drought phenomena. The aim at this study is to analyze the SPI and SPEI for determination of dry and wet meteorological periods and use of the SSI for the exploration of hydrological drought. The analysis of drought characteristics such as intensity and duration in three areas with different climates shows that the climate change has a major impact on the characteristics of the droughts. The relations between the duration and severity of drought have been more accurate in the period of 9 months in the Navroud watershed basin. The most significant events are SPI-9 with the duration of 57 months and the severity of 34.7, SPEI-9 with the duration of 34 months and the severity of 28.09 and SSI-9 with the duration of 41 months and the severity of 30.2. According to the obtained equations in different time periods, it was resulted that the highest accuracy was observed in the relationship between the meteorological and hydrological drought characteristics in the watershed basin of Segez for a period of 6 months. The results show that in all three basins, the correlation between the meteorological and hydrological drought is significant at the level of 99%. Results show that hydrological and meteorological droughts in Navroud and Lighvan basins have a significant correlation with 48-month periods and in the Seqez basin with 12- and 24-month periods, and the relations between hydrological droughts and meteorological droughts were obtained using the nonlinear linear models (polynomial, exponential and logarithmic). The good R^2 between the duration and severity of SPI-9 and SSI-9 is 0.8 and 0.92, respectively, for polynomial equations. The maximum determination coefficient of duration and severity of SPEI-9 and SSI-9 is 0.72 and 0.82, respectively, using polynomial equation. The application of several indices indicating different components of the hydrological cycle integrates many factors that affect and trigger droughts, and thus can help in providing a wider realization of the characteristics of droughts on various water sections.

Keywords Hydrological drought · Meteorological drought · SPI · SPEI · SSI

Introduction

Drought is one of the most common natural hazards that have an adverse effect on agriculture and water resources. Several drought indices have been developed to control the

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drought conditions. The drought indices have different characteristics and appropriate for specific environments. The physical relationship between the water cycle processes leads to the coordination of occurrence time and severity of hydrological and meteorological drought. Meteorological drought occurs rapidly, while hydrological drought occurs after a meteorological drought (Wilhite 2000). Drought indices such as PDSI (Palmer 1965), standardized evapotranspiration index (Vicente-Serrano et al. 2010) and standardized precipitation index (Mckee et al. 1993) are used extensively for monitoring the meteorological droughts over the world. Sims et al. (2002) studied the relationship between SPI with the soil moisture, which can determine the available water for plants and agriculture. The SDI is



based on the standardized river flow and surface flow and its computational principles are similar to SPI (Shukla and Wood 2008). Bazrafshan et al. (2010) calculated the SPI and RDI in eight costal stations of Iran, including five stations with very humid climate (located on the coast of the Caspian Sea) and three stations with very dry climate (located on the Persian Gulf coast), that there is a correlation of more than 0.9 between SPI and RDI in all stations and Student t test showed that there is no significant difference between two indices at a 5% confidence level. Edossa et al. (2010) studied the drought characteristics in the Awash River basin of Ethiopia based on meteorological and hydrological drought variables. The SPI was used for temporal and spatial analysis of meteorological drought and river stream flow was applied to the hydrological drought analysis and the results showed that the hydrological drought has lag 7 months than meteorological drought. Vicente-Serrano et al. (2011) investigated the possible impacts of warming processes on drought and water resources in Spain and showed that the precipitation and evapotranspiration increased over the period of 1930-2006 and SPI and SPEI had the same results. Tigkas et al. (2012) used RDI and SDI to study the impacts of weather conditions on the meteorological and hydrological droughts in the period of 3–12 months. The results showed that a high correlation was between the RDI-9 and SDI-12. Azareh et al. (2014) calculated the SPI and SDI. The results showed that the relationship between the drought impact on stream flow of the Karaj dam basin and the relationship between hydrological and meteorological drought is significant at 99% confidence level. Tokarczyk and Szalinska (2014) calculated the SPI and SRI in two basins of Poland. The results showed that the meteorological drought often related to hydrological drought. Ahmadalipour et al. (2017) analyzed the meteorological and hydrological drought of Willamette river basin in the Northwest Pacific basin. They used the atmospheric global circulation model of the GCMs and downscaling model of CMIP5 in order to assess the impact of climate change and used PRMS distributed hydrological model for simulation of rainfall-runoff. Results show that the meteorological drought can begin and end quickly, while hydrological drought takes much longer to develop and then recover. Wu et al. (2017) studied the hydrological and meteorological drought relationships using SPI and SSI in the Jinjiang river basin in China with consideration the impact of a large reservoir. They used to run theory to determine the drought characteristics from 1960 to 2010. They resulted that there is a nonlinear relationship between the hydrological and meteorological droughts. Wu et al. (2017) studied the effects of reservoir operation on the multiple correlations between the hydrological drought and meteorological droughts in the basin of the Dongjiang river in southern China (SPI) using monthly stream flow and precipitation data in 1960-2015 and the input and output stream flow of the Xinfengjiang reservoir in 1974–2009. The results showed that the reservoir operation from 1974 to 2015 has a positive impact on the short-term evolution of hydrological droughts (1 and 3 months). The aim of this present study is to investigate the dry and wet periods over three basins using the SPI, SPEI and SSI drought indices for long-term drought studies. The differences between three-index performances were discussed, and the relations between the indices were obtained using nonlinear models. The relationships between the indices are presented for the studied basins in the period of 1, 3, 6, 9, 12, 24 and 48 months. The main aim of this study is extraction of duration and severity of drought in the three watershed basins.

Materials and methods

Study area and data

In this research, three areas with several climates (dry, semiarid and wet) were used. The Lighvan watershed has the semiarid climate that is one of the most important sub-basins of Talkherood basin. It is in the province of East Azarbaijan, on the northern slopes of Sahand that extend between the geographic coordinates E longitude of 46° 25′-47° 26′ and N latitude of 37° 45′, Navroud basin has the wet climate that is one of the important watershed basins of the western province of Gilan in the city of Talesh between the E longitudes of 48° 35′-48° 54′ and N latitudes of 37° 36′-37° 45′ and originates in Alborz Mountain, which is part of Talesh Mountains and after joining the other sub-branches. The Seqez basin has the dry climate that climatology and hydrometric stations of Panbe dan valley were used that is located between the E longitude of 46° 17′ and N latitude of 36° 14′ from the equator. Figure 1 shows the geographic location of the meteorological and hydrometric stations, and Table 1 shows the geographic characteristics of the meteorological and hydrometric stations in studying basins. Table 2 presents annual statistics for each parameter stations.

Characteristics of used indices

Standardized precipitation index (SPI)

The standardized precipitation index (SPI) is a widely used index to characterize meteorological drought on a range of timescales. On short timescales, the SPI is closely related to soil moisture, while at longer timescales, the SPI can be related to groundwater and reservoir storage. The SPI can be compared across regions with markedly different climates. It quantifies observed precipitation as a standardized departure from a selected probability distribution function that models



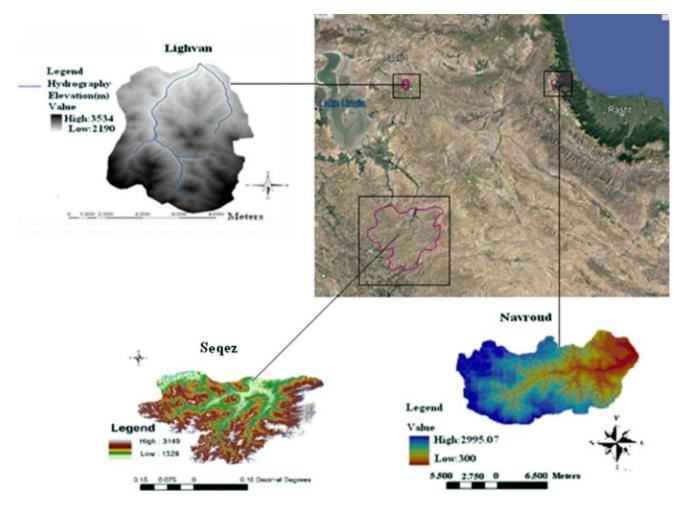


Fig. 1 Location of the study areas in Iran

 Table 1
 Information of hydrometric and meteorological stations

Station	Туре	Climate type	Area (km ²)	Elevation (m)	Longitude (degree)	Latitude (degree)
Navroud	Meteorological	Wet	274	807	48.73	37.67
Khalian	Hydrometric			142	48.73	37.67
Lighvan	Meteorological	Dry and semiarid	77	2279	46.43	37.83
Lighvan	Hydrometric			2200	46.43	37.83
Seqez	Meteorological	Mediterranean mountainous	4953.1	1522.8 1470	46.26 46.36	36.25 36.28
	Navroud Khalian Lighvan Lighvan	Navroud Meteorological Khalian Hydrometric Lighvan Meteorological Lighvan Hydrometric Seqez Meteorological	Navroud Meteorological Wet Khalian Hydrometric Lighvan Meteorological Dry and semiarid Lighvan Hydrometric Seqez Meteorological Mediterranean mountainous	Navroud Meteorological Wet 274 Khalian Hydrometric Lighvan Meteorological Dry and semiarid 77 Lighvan Hydrometric Seqez Meteorological Mediterranean mountainous 4953.1	Navroud Meteorological Wet 274 807 Khalian Hydrometric 142 Lighvan Meteorological Dry and semiarid 77 2279 Lighvan Hydrometric 2200 Seqez Meteorological Mediterranean mountainous 4953.1 1522.8	Navroud Meteorological Wet 274 807 48.73 Khalian Hydrometric 142 48.73 Lighvan Meteorological Dry and semiarid 77 2279 46.43 Lighvan Hydrometric 2200 46.43 Seqez Meteorological Mediterranean mountainous 4953.1 1522.8 46.26

the raw precipitation data (McKee et al. 1993). The raw precipitation data are typically fitted to a gamma or a Pearson type III distribution and then transformed to a normal distribution. The SPI values can be interpreted as the number of standard deviations by which the observed anomaly deviates from the long-term mean. The SPI can be calculated (Eq. 1) for differing periods of 1–36 months, using monthly precipitation data. In the operational community, the SPI has

been recognized as the standard index that should be available worldwide for quantifying and reporting meteorological drought. Concerns have been raised about the utility of the SPI as a measure of changes in drought associated with climate change, as it does not deal with changes in evapotranspiration. Alternative indices that deal with evapotranspiration have been proposed. Ultimately, the SPI value is calculated by converting the cumulative probabilities based



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Table 2 Annual statistics for each parameter

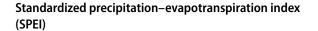
Basin	Parameter	Evapotran- spiration (mm/day)	Discharge(m ³ /s)	Pre- cipitation (mm)
Seqez	Number of data	300	300	300
	Average	114.3	8.16	37.82
	Min	20.65	0.044	0
	Max	248.9	78.19	354.1
	Standard deviation	63.81	11.8	43.65
	Skewness	0.19	2.57	2.23
	Kurtosis	- 1.33	8.7	9.77
Ligvan	Number of data	300	300	300
	Average	110.34	0.8	29.6
	Min	24.52	0.078	0
	Max	304.08	5.3	143.3
	Standard deviation	60.93	0.86	25.39
	Skewness	0.36	2.6	1.22
	Kurtosis	- 1.03	7.7	1.26
Navroud	Number of data	300	300	300
	Average	65.80	1.86	56.72
	Min	13.54	0.7	2
	Max	167.9	7.08	271.9
	Standard deviation	45.2	0.94	36.37
	Skewness	0.07	1.94	1.47
	Kurtosis	- 1.5	5	4.4

on the Gamma distribution to a standard normal distribution (McKee et al. 1993). The SPI can be calculated as follows:

SPI =
$$s \frac{t - (c_2 t + c_1)t + c_0}{((d_3 t + d_2) + d_1) + 1}$$
 $t = \sqrt{\ln \frac{1}{H(X)^2}}$ (1)

$$G(x) = \frac{1}{\beta^{\gamma} \Gamma(\gamma)_0} \int_0^x X^{\gamma - 1} e^{\frac{-x}{\beta}} dx, \quad X > 0(\gamma) = \int_0^\infty X^{\gamma - 1} e^{-x} dx$$
(2)

where x denotes precipitation value; b and c represent the scale and shape parameters of the C function; S is positive and negative coefficients; and c_0 , c_1 , c_2 and d_1 , d_2 , d_3 are calculated parameters. Their values are displayed as follows: c_0 =2.515517, c_1 =0.802853, c_2 =0.010328, d_1 =1.432788, d_2 =0.189269 and d_3 =0.001308. G(x) denotes the probability distribution of precipitation. When G(x)>0.5, then H(x)=1-G(x) and S=1; otherwise, H(x)=G(x) and S=-1.



FAO-56 illustrated Penman–Monteith's method as the standard method for calculating the reference evapotranspiration (Alan et al. 1998):

$$ET_{0} = \frac{0.408\Delta(R_{n} - G) + \gamma \left[\frac{890}{T + 273}\right] U_{2}(e_{a} - e_{d})}{\Delta + \gamma (1 + 0.34U_{2})}$$
(3)

where ET₀ represents the evapotranspiration of plant (mm/day), $R_{\rm n}$ is the net radiation on vegetation cover (megajoul/m²/day), T is the average air temperature (C), U₂ introduces the wind speed at 2 m above the ground level (m/s), $e_{\rm a}-e_{\rm d}$ shows the pressure shield shortage at 2 m (kPa), Δ is determined by the slope of the vapor pressure curve (kPa/C), γ is the psychometric coefficient (kPa/C) and G is the heat flux into the soil (Mj/m²/day).

The SPEI is presented by Vicente-serrano et al. (2011) and it has been used in numerous studies; also calculation method involves the equilibrium of the climate and considers the role of the temperature in the drought evaluation. Previously, the palmer drought severity index (PDSI) uses the readily available temperature and precipitation data to estimate relative dryness (Palmer 1965). It is a standardized index that spans - 10 (dry)-+10 (wet) (Vicente-serrano et al. 2010). It has been reasonably successful at quantifying long-term drought. As it uses temperature data and a physical water balance model, it can capture the basic effect of global warming on drought through changes in potential evapotranspiration. Some studies have compared different methods for calculating PET (Sheffield et al. 2012) and it has been shown that the Penman–Monteith equation approximates net evapotranspiration (ET), requiring as input daily mean temperature, wind speed, relative humidity and solar radiation (Allen et al 1998). Therefore, in this study the calculation of SPEI is based on Penman-Monteith equation with Hargreaves-Samani correction that described in FAO-56 (Allen et al. 1998). The PM method chosen by the World Meteorological Organization (WMO) that has been proposed as the standard method for PET estimation, and its accuracy has been proved by the need of less data.

The monthly values of the reference plant evapotranspiration are calculated based on the climatological data and using Eq. (3). In the next step, the difference between the precipitation (P) and evapotranspiration (ET_0) for the ith month can be calculated:

$$D_i = P_i - \text{PET}_{0i} \quad i = 1, 2,, N$$
 (4)

In order to calculate SPEI in different timescales, it is necessary to form series at different time steps (Paulo et al. 2003):



$$\begin{aligned} x_{i,j}^{k} &= \sum_{l=13-k+j}^{12} w_{i-1+l} + \sum_{l=1}^{j} w_{i,l} & \text{if} \quad j < k \\ x_{i,j}^{k} &= \sum_{l=i-k+1}^{j} w_{i,l} & \text{if} \quad j \ge k \end{aligned} \tag{5}$$

where $w_{i,1}$ is the value of D_i or the water requirement in the first month of the year (mm). The SPEI is used at various times for monitoring the agricultural and hydrological droughts (komuscu, 1999). The SPEI calculating, like the SPI method, requires estimating cumulative probability values of D_i by fitting a probability function. Now, D_i values from the lower bound lead to the negative values and two-parameter probability functions cannot be selected. In this research, with goodness-of-fit test, extreme value distribution function was selected for D_i series and the drought analysis was performed on time steps of 3, 6, 9, 12, 24 and 48 months. The crossover probability values of D_i series are converted to the standardize function with mean zero and standard deviation of 1, which will be equal to the values of SPEI (Vicente-Serrano 2006):

SPEI =
$$W - \frac{C_0 + C_1 W + C_2 W^2}{1 + d_1 W + d_2 W^2 + d_3 W^3}$$
 (6)

$$W = \sqrt{-2\operatorname{Ln}(p)} \text{ for } P \le 0.5 \tag{7}$$

in which P is the probability of exceeding the D and P = 1-F(x) values. If the value of P is greater than 0.5, then the value of P is replaced with 1-P and SPEI sign is changed.

Standard stream flow index (SSI)

The researchers developed the standard hydrological drought indices similar to the meteorological drought indices. Two known hydrological drought indices, which include standard stream flow index and stream flow drought index, have the same theoretical background (Shukla and Wood 2008). Both indices attempt to convert the monthly flow into a standard normal distribution (mean zero and variance of one, similar to SPI method) and calculate the hydrological drought index. In this research, the standardized flow index was used. The SSI is calculated based on nonparametric approach. Therefore, in order to calculate this index, exactly the same calculation process is repeated; only with the difference that instead of precipitation data, stream flow data are used as input data. For this index, as same SPI, the gamma distribution is appropriate. This method is simple and similar to SPI method. The cumulative flow values for each month are individually evaluated, and SSI is calculated for each month. The classification of the indices used in this study is shown in Table 3.

Table 3 Classification of different states of drought indices (McKee et al. 1993)

Drought category	SPI, SPEI, SSI		
Extremely wet	>2		
Very wet	1.5-1.99		
Moderately wet	1-1.49		
Near normal	- 0.99-0.99		
Moderately dry	-1 to -1.49		
Severely dry	- 1.5 to - 1.99		
Extremely dry	- 2 and less		

Evaluation criteria

In this study, Pearson correlation coefficient (Cercal Pearson) and crossover correlation function (Chang et al. 1997) were used to evaluate the comparative indices. The coefficient of determination (Draper and Smith 1998) was used in order to evaluate the efficiency of mathematical relations between indices. Table 4 shows the equations of the accuracy indices.

Drought identification using run theory

Yevjevich (1967) suggested the run theory (Fig. 2), which has been used often in time series of anomalous hydrological events and was used to identify drought components and survey their statistical properties (Mishra and Desai 2005; Nam et al. 2015). A drought phenomenon is defined as a continuing sequence of months (t) with drought index value (X_t) less than a selected threshold (X_0) . A drought event is defined by the following components, which can be applied for mathematical analysis of drought (Fig. 2). Drought beginning time (T_s) is the onset month of a drought event. Drought ending time (T_e) shows the date when the shortage of water becomes sufficiently small so that the drought no longer persists. Drought duration (D) is the time period between the starting and ending of a drought. Drought severity (S) is obtained by the cumulative shortage of the drought parameter below the critical level. Drought intensity (I) is calculated as the proportion of drought severity and the drought duration. Figure 2 shows the characteristics of the drought using the run theory (Yevjevich 1967).

Results and discussion

Comparative evaluation of the meteorological drought and hydrological drought

For comparative evaluation of the meteorological and hydrological drought indices, graphs of SPI and SSI, and



Accuracy index	Equation	Range
Pearson correlation coefficient	$R = \frac{(\sum_{i=1}^{t} (x_i y_i) - (\sum_{i=1}^{t} x_i)(\sum_{i=1}^{t} y_i)}{\sqrt{\left[n(\sum_{i=1}^{t} (x_i^2)) - (\sum_{i=1}^{t} x_i)^2\right] \left[n(\sum_{i=1}^{t} (y_i^2)) - (\sum_{i=1}^{t} y_i)^2\right]}}$	$-1 \le R \le +1$
Crossover correlation function	$R = \frac{\sum_{i}^{n=1} (x_{(i)} - \bar{x})(y_{(i-d)} - \bar{y})}{\sqrt{\sum_{i=1}^{n} (x_{(i)} - \bar{x})\sqrt{\sum_{i=1}^{n} (x_{(i)} - \bar{x})^{2}} \sqrt{\sum_{i=1}^{n} (y_{(i-d)} - \bar{y})^{2}}}}$	$-1 \le R \le +1$
R^2	$R^{2} = \left[\frac{\sum_{N}^{l=1} (x_{i} - \bar{x})(y_{i} - \bar{y})}{\sqrt{\sum_{N}^{l=1} (x_{i} - \bar{x})^{2} (\sum_{N}^{l=1} (y_{i} - \bar{y}))^{2}}} \right]^{2}$	$0 \le R^2 \le +1$

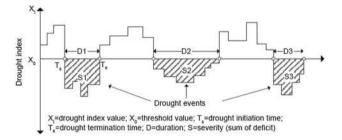


Fig. 2 Definition of drought characteristics including duration and magnitude using the run theory (Yevjevich 1967)

SPEI and SSI in the three studied watershed basins are plotted (1992–2016). Figure 3 shows the Pearson correlation between SPI, SPEI and SSI at 1–48 months' time steps. Significant positive correlation means that the decrease in the precipitation causes the decrease in the stream flow; in other words, meteorological droughts in the watershed basin caused a hydrological drought throughout the basin. There is a good correlation between 48 months of SSI-SPI and SSI-SPEI in Navroud basin. The maximum correlation between 24 months of SSI-SPI and 12 months of SPEI-SSI is observed in Seqez basin.

Figure 3 shows the Pearson correlation between SPI-SPEI and SSI-SSI drought indices during the period of 1–48 months in the studied basins.

in the Navroud basin is between SPI and SSI at lags 3 and 4 in the 48-month period with the values of 0.730 and 0.731, respectively. It means that the meteorological drought in the Navroud basin affects the hydrological drought at lags 3 and 4 and the maximum correlation observed for a period of 48 months and between SPEI and SSI at lags 1 and 2 with the values of 0.687 and 0.686, respectively. In other words, the hydrological drought in Navroud basin responds to the meteorological drought at lags 1 and 2. Figure 4 shows the crossover correlation between SSI-SPI and SSI-SPEI simultaneously. As shown in Fig. 4, the maximum correlation observed in Navroud basin in the 48-month period and good crossover coefficient was between SPI and SSI with a value of 0.527 at lag 7 in the period of 48-month period. It means that the hydrological drought has occurred to the meteorological drought with the 7 lag months. These results similar to what was found by Edossa et al. (2010) in the Awash river basin of Ethiopia. It means that the meteorological and hydrological droughts occur in a basin at lags 7 months. Also, Fig. 4 shows the good correlation in the 48-month period. According to the results, in Seqez basin, the maximum correlation coefficient between SPI and SSI was obtained instantaneously in the 24-month period with the value of 0.614. This means that the meteorological drought in the region affects immediately the surface water and the crossover coefficient between SPEI and SSI in this

Based on the results, the highest correlation coefficient

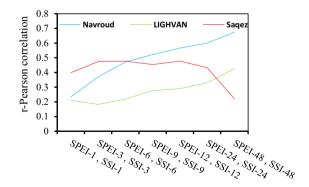
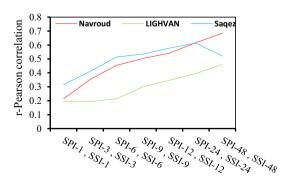


Fig. 3 Pearson correlation coefficients between indices for 1–48 months





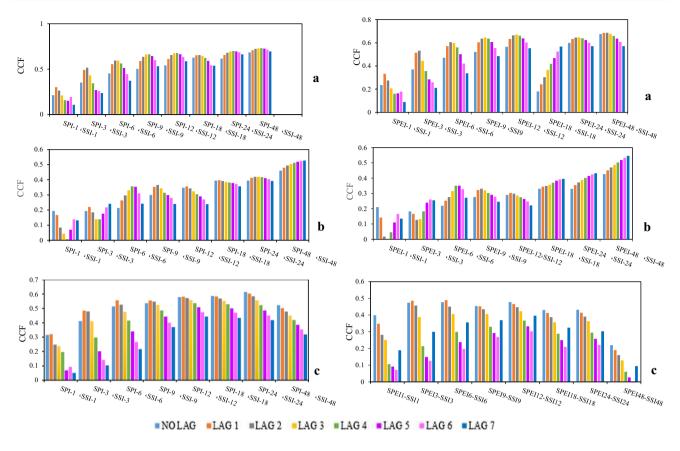


Fig. 4 Crossover correlation between indices simultaneously in the a Navroud, b Lighvan, c Seqez

basin was observed in the 6-month period at lag 1 month with the value of 0.489. In other words, the meteorological drought in the region is affected the surface water resources at lag 1 month.

Figure 5 Shows the time series of drought indices with high cross-correlation coefficient in the study areas.

Extraction of relationship between the indices

In this research, SPI, SSI and SPEI from 1992 to 2016 were calculated and the characteristics of meteorological and hydrological drought were extracted using the Run theory. The relations between hydrological droughts and meteorological droughts were obtained (Table 5) using the nonlinear models (polynomial, exponential and logarithmic). The relationships between the indices are presented for the studied basins in the period of 1, 3, 6, 9, 12, 24 and 48 months. The relations between the duration and severity of drought have been more accurate in the period of 9 months in the Navroud watershed basin. The most significant events are SPI-9 with the duration of 57 months and the severity of 34.7, SPEI-9 with the duration of 34 months and the severity of 28.09 and SSI-9 with the duration of 41 months and the severity of 30.2. The good R^2 between the duration and severity of

SPI-9 and SSI-9 is 0.8 and 0.92, respectively, for polynomial equations. The maximum determination coefficient of duration and severity of SPEI-9 and SSI-9 is 0.72 and 0.82, respectively, using polynomial equation. Also Table 4 shows that a polynomial function is better than to other functions in Navroud hydrometric station. The calculated relations between the duration and severity of indices show that the good accuracy is in the period of 12 months in the watershed basin. The most important events are SPI-12 with the duration of 88 months and the severity of 100.98, SPEI-12 with the duration of 88 months and the severity of 93.11 and SSI-12 with the duration of 47 months and severity of 60.22. According to Table 4, the highest accuracy between SPI-12 and SSI-12 is related to exponential and logarithmic equations with $R^2 = 0.99$ and $R^2 = 0.92$, respectively, and the highest R² between the duration and severity of SPEI-12 and SSI-12 is related to the logarithmic and exponential equations and equals to 0.9. According to the obtained equations in different time periods, it was resulted that the highest accuracy was observed in the relationship between the meteorological and hydrological drought characteristics in the watershed basin of Seqez for a period of 6 months. The most important events are SPI-6 with the duration of 36 months and the severity of 33.8, SPEI-6 with the duration



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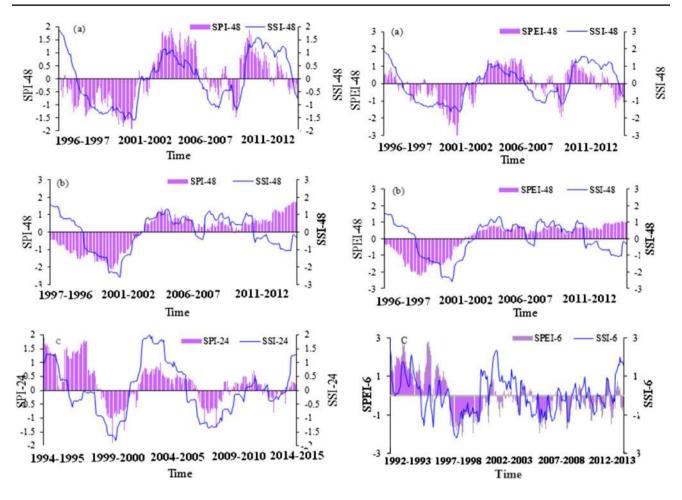


Fig. 5 Time series of drought indices with high cross-correlation coefficient in the a Navroud, b Lighvan, c Seqez

of 56 months and the severity of 34.8, and SSI-6 with the duration of 37 months and the severity of 41.22. Regarding the severity and duration of SPI-6 and SSI-6, the highest accuracy was obtained by polynomial equation with the determination coefficient of 0.98 and 0.95, respectively, and the highest R² between the severity and duration of SPEI-6 and SSI-6 for the exponential and polynomial equations is 0.98 and 0.79, respectively.

Conclusion

Iran is in the temperate (arid and semiarid) zone of the world. The use of drought indices allowed studying and analysis of the characteristics and propagation behaviors of droughts using SPI, SPEI and SSI for extracting the time series of dry and wet periods during past periods. From the computation and analysis of these indices at meteorological and hydrometric stations in study areas, we observed that droughts from 1992 to 2016 were depicted by these indices based on the meteorological and hydrological data. The SPEI is more appropriate than the SPI

for applications examining of drought variability in study areas because it uses precipitation and evapotranspiration data. The results showed that precipitation plays a significant role in explaining the time variations of the droughts and temperature increasing also has a significant effect on the water shortage, especially in long-term periods in the region. The Pearson correlation matrix and crossover correlation show that SPI drought index is better than SPEI drought index in the Navroud basin because Navroud basin is wet zone and with less evapotranspiration. However, the SSI hydrological drought index responds faster to SPEI drought index (lags 1 and 2) compared to SPI (lags 3 and 4). In the arid and semiarid areas, because of much evapotranspiration, the SPEI is better than the SPI and it was found that SSI has responded to both SPI and SPEI in the watershed basin at lag 7. Extracting the nonlinear model between the meteorological and hydrological drought shows that there is a relationship between the hydrological drought response to the meteorological drought. In general, the application of several indices indicating different components of the hydrological cycle integrates many factors that affect and trigger droughts, and thus can help



Table 5 Relationships of hydrological drought and meteorological drought

Station	Index	Duration	R^2	Magnitude	R^2
Navroud S	SPI-9, SSI-9	$SSI_D = 28.8 \text{ SPI}_D^{-0.0122}$	0.6	$SSI_{M} = 10.9 SPI_{M}^{0.192}$	0.57
		$SSI_D = 23.4 e^{0.0067} SPI_D$	0.5	$SSI_M = 12.4 e^{0.0173 SPI}_M$	0.4
		$SSI_D = 49.5-6.44 SPI_D + 0.295 SPI_D^2 - 0.00328 SPI_D^3$	0.8	$SSI_M = 12.7-2.61 \text{ SPI}_M + 0.25 \text{ SPI}_M^2 - 0.00491 \text{ SPI}_M^3$	0.92
		$SSI_D = 28.5 - 0.245 \text{ LN}(SPI_D)$	0.6	$SSI_{M} = 10.5 + 3.1 \text{ LN(SPI}_{M})$	0.6
	SPEI-9, SSI-9	$SSI_D = 4.5 \text{ SPEI}_D^{0.597}$	0.48	$SSI_{M} = 2.1 \text{ SPEI}_{M}^{0.75}$	0.57
		$SSI_D = 11.6 e^{0.036SPEI}_D$	0.44	$SSI_{M} = 7.6 e^{0.0433} SPEI_{M}$	0.42
		$SSI_D = -17.5 + 8.17 \text{ SPEI}_D - 0.504$ $SPEI_D^2 + 0.00938 \text{ SPEI}_D^3$	0.72	$SSI_{M} = 3.4-1.64 \text{ SPEI}_{M} + 0.313 \text{ SPEI}_{M}^{2} - 0.00835 \text{ SPEI}_{M}^{3}$	0.82
		$SSI_D = -10.69 + 13 LN(SPEI_D)$	0.5	$SSI_{M} = -12.6 + 11.1 LN(SPEI_{M})$	0.63
Lighvan SPI-12,	SPI-12, SSI-12	$SSI_D = 4.77 \text{ SPI}_D^{0.511}$	0.91	$SSI_{M} = 2.8 SPI_{M}^{0.665}$	0.99
		$SSI_{D} = 13.7e^{0.0139x}$	0.90	$SSI_M = 7.28e^{0.02092} SPI_M$	0.98
		$SSI_D = -19 + 14.8 \text{ LN(SPI}_D)$	0.92	$SSI_{M} = 0.74 + 0.906 SPI_{M} + 0.081 SPI_{M}^{2}$	0.98
		$SSI_D = (4.28 \times 10^{-12}) - 5.56 \text{ SPI}_D + 0.742 \text{ (SPI}_D$	0.90	$SSI_{M} = -14.5 + 15.5LN(SPI_{M})$	0.94
	SPEI-12, SSI-12	$SSI_D = 7.22 \text{ SPI}_D^{0.422}$	0.70	$SSI_{M} = 4.46 \text{ SPEI}_{M}^{0.573}$	0.99
		$SSI_D = 17.1 e^{0.0118 SPI}_D$	0.68	$SSI_{M} = 7.56 e^{0.0233} SPEI_{M}$	0.98
		$SSI_D = (4.27 \times 10^{-11}) - 3.5 \text{ SPI}_D + 0.581 \text{ SPI}_D^2$	0.67	$SSI_{M} = -0.968 + 9.45 \text{ SPEI}_{M} - 1.8 \text{ SPEI}_{M}^{2}$	0.98
		$SSI_D = -12.1 + 1.34 LN(SPI_D)$	0.99	$SSI_M = -2.25 + LN(SPEI_M)$	0.91
Seqez	SPI-6, SSI-6	$SSI_D = 1.93 \text{ SPI}_D^{8.27}$	0.77	$SSI_{M} = 0.755 SPI_{M}^{1.14}$	0.97
		$SSI_D = 7.17 e^{0.0461 SPI}_D$	0.89	$SSI_{M} = 4.82 e^{6.53 SPI}_{M}$	0.62
		$SSI_D = 19.7-3.77 SPI_D + 0.32 SPI_D^2 - 0.00556 SPI_D^3$	0.95	$SSI_{M} = 4.7-0.6 \text{ SPI}_{M} + 0.123 \text{ SPI}_{M}^{2} - 0.00216 \text{ SPI}_{M}^{3}$	0.98
		$SSI_D = -17 + 14.6 LN(SPI_D)$	0.88	$SSI_{M} = -13.3 + 13.1 \text{ LN(SPI}_{M})$	0.78
	SPEI-6, SSI-6	$SSI_D = 0.15X^{1.4}$		$SSI_M = 0.393 \text{ SPEI}_M^{1.2}$	0.98
		$SSI_D = 5.17e^{0.0366X}$	0.76	$SSI_{M} = 5.16e^{0.0403 \text{ SPEI}}M$	0.9
		$SSI_D = 16.3 - 2.33X + 0.11X^2 - 0.00111X^3$		$SSI_{M} = -1.93 + 0.352 \text{ SPEI}_{M} + 0.031 \text{ SPEI}_{M}^{2}$	0.94
		Y = -29.4 + 15.4 LN(X)	0.6	$SSI_{M} = -36.9 + 19 LN(SPEI_{M})$	0.96

in providing a wider realization of the characteristics of droughts on various water sections.

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Compliance with ethical standards

Conflict of interest The authors have no conflicts of interest to declare.

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