

ORIGINAL ARTICLE

Simultaneous Model Order and Parameter Estimation (SMOPE) based on Random Asynchronous Particle Swarm Optimization

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ABSTRACT – Simultaneous model order and parameter estimation (SMOPE) is a metaheuristic based system identification method. SMOPE was introduced using particle swarm optimization (PSO). There are several iteration strategies for PSO. The original work on SMOPE is based on synchronous PSO (S-PSO). However, in some works PSO using other iteration strategy is found to give better results. In this work, based on six system identification problems random asynchronous (RA-PSO) based SMOPE is found to have slight advantage over S-PSO.

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Introduction

Simultaneous model order and parameter estimation (SMOPE) was proposed for solving autoregressive exogenous system identification problem effectively using metaheuristics algorithms [1-2]. The method enabled a system's order and parameters values to be searched simultaneously. This is possible through the way the problem is encoded in the search agents. Even though SMOPE was introduced based on particle swarm optimization (PSO) [1-2], it can easily be adapted to suit other metaheuristic algorithm such as, gravitational search algorithm (GSA) [3-4].

The PSO is a population-based optimization algorithm. The search agents of PSO, known as particles mimics how living organism such as birds and fishes look for food by exploring the search area using their own experience and information from neighborhood as guidance. The search in PSO is done iteratively. PSO's iteration strategy can be classified as synchronous (S-PSO) and asynchronous (APSO) update [5]. S-PSO is more popular approach than A-PSO, where in S-PSO the movement of the whole particles in the swarm is done at once, after their performance is evaluated. In A-PSO a particle moves as soon as its own performance is evaluated, without the need to wait for others to complete their evaluation. The direction of the movement in A-PSO is made based on whatever information available. This is a more accurate replication of nature.

Random asynchronous PSO (RA-PSO) was introduced in [6]. In the original APSO the particles

are evaluated and move according to the particle number. However, in RA-PSO the particle to be evaluated and move is chosen randomly, hence, in an iteration a particle can move more than once or none at all. It is found that RA-PSO is better than A-PSO.

In this work the implementation of SMOPE using RA-PSO is studied and compared with SMOPE based on S-PSO. In several works, implementation of PSO with a particular iteration strategy is found to give a better result compare to other strategy. For example, Wu and Gao had reported that their adaptive inertia weight PSO implemented using asynchronous update has a better performance than the same approach implemented using synchronous update [7]. In [8], A-PSO with discrete crossover is found to perform better than S-PSO with the crossover operator.

However, Engelbrecht in his work concluded that there is no definite winner of S-PSO vs A-PSO but rather it is a function dependent option [5]. The same observation is made in [9].

Therefore, in this work the performance of RA-PSO based SMOPE is compared with the S-PSO based SMOPE. Six ARX system identification problems are used. The results show that RA-PSO on average has a slightly better performance.

Autoregressive Exogenous Model (ARX)

System identification is a task of finding an accurate mathematical model of a control system based on the available input and output data [10]. In [11], the ARX model was introduced by Ljung among many other models for system identification.

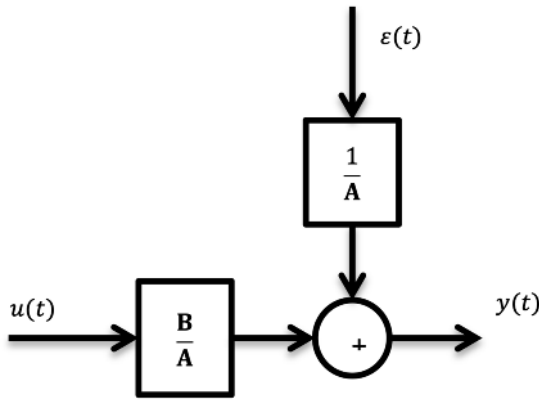


Figure 1. The ARX structure.

The ARX structure is presented in Figure 1. In the figure, $u(t)$ and $y(t)$ represent input and output of the model. The term $\varepsilon(t)$ represents white noise that enters the system as direct error. The mathematical model for ARX is:

$$y(t) + a_1y(t-1) + a_2y(t-2) + \dots + a_{m_a}y(t-m_a) = b_1u(t-1) + b_2u(t-2) + \dots + b_{m_b}u(t-m_b) + \varepsilon(t) \quad (1)$$

where

$$\mathbf{A} = \{a_1, a_2, \dots, a_{m_a}\} \quad (2)$$

$$\mathbf{B} = \{b_1, b_2, \dots, b_{m_b}\} \quad (3)$$

are the tunable parameters. Applying z-transform the transfer function can be written as:

$$G(z) = \frac{Y(z)}{U(z)} = \frac{b_1z^{-1} + b_2z^{-2} + \dots + b_{m_b}z^{-m_b}}{1 + a_1z^{-1} + a_2z^{-2} + \dots + a_{m_a}z^{-m_a}} \quad (4)$$

The system identification problem is optimized when the best values of the tunable parameters, which are the poles and zeros parameters are found.

SMOPE

In contrast to other system identification approaches, SMOPE find the optimal system order and the parameters values simultaneously. In [1], standard PSO was chosen to search for optimal system order and parameters values.

The key of SMOPE is the encoding of the search agents. Therefore, by adopting similar encoding, SMOPE can easily be applied to other optimization algorithms such as GSA [3-4]. The agent's encoding used in SMOPE is shown in Table 1.

Each of the agents in SMOPE represents system order and parameters values. Assuming maximum system order under consideration is D , the agents dimension should be $2D+1$. The first dimension of each agent's represents the system order; n , while dimension 2 to $D+1$ represents the possible values of poles parameters, a_1, a_2, \dots, a_{m_a} and dimension $D+2$ to $2D+1$ are reserved for the zeros parameters, b_1, b_2, \dots, b_{m_b} . Both m_a and m_b can be lesser than D . If $m_a < D$, then only the values in dimension 2 to m_a+1 are used, while the values in dimension m_a+2 to $D+1$ are ignored. Similarly, if $m_b < D$, then only the values in dimension $D+2$ to $D+m_b+1$ are used, while the values in dimension $D+m_b+2$ to $2D+1$ are ignored. In this work the maximum order considered is 9 with $m_a \leq m_b$.

Particle Swarm Optimization

Particle swarm optimization (PSO) is a population based algorithm which has gain popularity due to its simplicity and low computational cost. It has been successfully adapt in various fields, such as robotics [12], power distribution planning [13], and financial planning [14].

Each of the particles in PSO acts as the search agents. The particles has velocity, and position, . The search for optimal solution is conducted in PSO by iteratively evaluating and updating particles performance, velocity and position. The velocity and position are updated according to equation (5) and (6), accordingly. The particles' search direction is influenced by the previous search, their own best performance, $pBest_i$, and neighbourhood best, $gBest$. The performance of the particles' can be measured using equation (7). In the equation, $\hat{y}_{(estimation)}$ is the output signal based on the mathematical model found by a particle, whereas y is the actual data and \hat{y} is its mean value.

In this paper, SMOPE is implemented using PSO of two different update strategies, synchronous PSO (S-PSO) and random asynchronous PSO (RA-PSO).

$$v_i(t) = \omega v_i(t - 1) + c_1 r_1 (pBest_i - x_i(t - 1)) + c_2 r_2 (gBest - x_i(t - 1)) \tag{5}$$

$$x_i(t) = v_i(t - 1) + x_i(t - 1) \tag{6}$$

$$best\ fit = 100 \left[1 - \frac{norm(\hat{y}_{estimation} - y)}{norm(y - \hat{y})} \right] \% \tag{7}$$

Synchronous update is the more famous iteration strategy for PSO. In S-PSO, the whole population is updated first before their velocities and positions are updated. Hence, the particles have overview of the whole swarm’s performance before the next move is made. The pseudocode for S-PSO is shown in Figure 2. There are two loops per iteration for S-PSO. In the first loop the performance of the whole population is evaluated, whereas the particles velocities and positions are updated in the second loop.

Random asynchronous update is a new iteration strategy for PSO [5]. In RA-PSO, a particle is chosen randomly to be evaluated. Immediately after this particle is evaluated, its velocity and position are updated using the available information. There is no restriction on repetition, hence a particle can be chosen more than once or none at all in an iteration. The chosen particles in RA-PSO are updated based on various neighbourhood information. The pseudocode for RA-PSO is shown in Figure 3. There is only one loop per iteration in RA-PSO. In the loop, first a particle to be evaluated is randomly chosen, then its performance is evaluated, followed by its velocity and position update.

Experiments

Six system identification problems found in database for the identification of system (DaISy) were used. Four of the systems chosen are mechanical systems, which are ball-beam, hair-dryer, wing flutter and robot arm. The data for ball-beam, hairdryer and robot arm systems are obtained from laboratory works while the wing flutter data is obtained from industry. A thermic system namely SISO heating system is also chosen for the experiment. The heating system’s output is measured using thermocouple taken from the back of a steel plate. The last experiment is using data from process industry, which is a liquid-saturated steam heat exchanger system.

The first half of the data from each of the systems, is used for training purposed, which is to select the best order and parameters values using SMOPE, while the other half is used for testing.

For example, as shown in Figure 4. The first half of the data for the hair dryer system (in the box) is used for training while the remaining is used to test the quality of the solution found by SMOPE.

Table 1. Agent’s encoding.

Dimension	Variable in ARX
1	Order, n
2	a_1
3	a_2
...	...
$D+1$	a_D
$D+2$	b_1
$D+3$	b_2
...	...
$2D+1$	b_D

```

1. Random initialization of swarm
2. do
3.   for all particles
4.     evaluate performance
5.     update pBest and gBest
6.   end
7.   for all particles
8.     update velocity
9.     update position
10.  end
11. while stopping condition is not achieved
    
```

Figure 2. S-PSO’s pseudocode.

```

12. Random initialization of swarm
13. do
14.   for number of particles
15.     randomly choose a particle
16.     evaluate performance
17.     update pBest and gBest
18.     update velocity
19.     update position
20.   end
21. while stopping condition is not achieved
    
```

Figure 3. RA-PSO’s pseudocode.

The SMOPE method is implemented using both S-PSO and RA-PSO here. The algorithms are using population of 100 particles which are randomly initialized. The algorithms are repeated until either 100% training fitness is achieved or the iteration count exceeds 2000. Each of the experiment is repeated 50 times and the results found are averaged.

Results and Discussions

The results obtained from the experiment are tabulated in Figure 5 and Figure 6 shows the average training fitness in every iteration for each system.

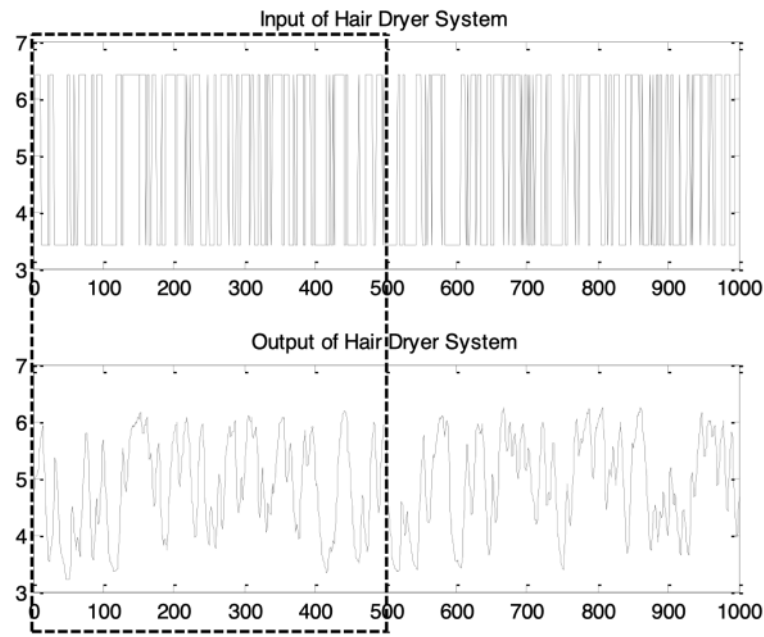


Figure 4. Input and output data of the hair dryer system.

Data Set	Best Fit (Training) (%)				Average Best Fit (Training) (%)				STDEV (Training)				Best Fit (Testing) (%)				Average Best Fit (Testing) (%)				STDEV (Testing)											
	Min		Max		Min		Max		Min		Max		Min		Max		Min		Max		Min		Max									
	S-PSO	RA-PSO	S-PSO	RA-PSO	S-PSO	RA-PSO	S-PSO	RA-PSO	S-PSO	RA-PSO	S-PSO	RA-PSO	S-PSO	RA-PSO	S-PSO	RA-PSO	S-PSO	RA-PSO	S-PSO	RA-PSO	S-PSO	RA-PSO	S-PSO	RA-PSO								
Heating System	98.688	98.542	99.050	99.086	98.9185	98.9465	0.131342	0.130077	97.952	97.843	98.752	98.809	98.4394	98.5029	0.27228	0.24904	9503	5263	822	16293	545	397	98	697	34289	96044	76804	92534	4718	7061	8117	269
Hair Dryer System	87.283	87.283	95.293	95.221	90.1863	90.6040	2.418449	2.712445	86.661	86.661	95.233	95.216	89.9372	90.3474	2.56124	2.88425	54613	54613	08609	51301	4857	7414	634	3	686	686	41803	20629	3484	4069	1337	9043
Robot Arm System	90.891	90.891	97.624	98.018	95.7206	95.3209	1.679574	2.346756	90.549	90.549	97.534	97.953	95.5848	95.1632	1.74418	2.43825	11807	11807	46453	74249	826	7306	667	688	79568	94946	95163	0968	0162	249	8671	
Wing Flutter	96.764	96.764	99.046	99.104	98.1638	98.2321	0.740067	0.836681	90.319	90.319	96.807	96.935	93.6405	93.9698	2.04784	2.30247	7563	7563	0994	4069	475	7188	68	164	82512	41887	90385	1679	7304	0589	8218	
Ball Beam	96.484	96.484	97.463	97.467	97.2077	97.1980	0.184859	0.192925	96.575	96.575	97.823	97.819	97.4798	97.4652	0.24139	0.25395	37085	37085	63029	99711	2236	2756	727	859	86006	74866	36721	6053	3921	9928	1298	
Exchanger System	80.256	80.256	81.019	80.934	80.6598	80.6724	0.292140	0.295281	49.417	49.417	50.412	50.414	50.0094	50.0307	0.43442	0.43552	4027	4027	2168	8651	087	73	31	28	39614	39615	10458	21039	0316	8219	5592	9237

Figure 5. Performance of S-PSO based SMOPE vs RA-PSO based SMOPE.

On average RA-PSO has a slight advantage over the original implementation which is based on S-PSO. Out of the six systems used, RA-PSO performs better in four systems, which are the heating system, exchanger system, hair dryer system and wing flutter system. RA-PSO has a better performance for these systems in training phase as well as in the testing stage. However, the differences between the two algorithms are marginal.

The marginal difference can be seen in Figure 5. It can be seen that in all iteration the fitness of S-PSO based SMOPE and RA-PSO based SMOPE is close to each other. The mathematical models for each system found by both algorithms are presented in Figure 7.

Both algorithms found their own model with their own parameters values and system order.

Conclusion

SMOPE is a metaheuristic based system identification method. The method is able to determine the system order and the parameters simultaneously. This work investigates the difference between S-PSO based and RA-PSO based SMOPE. The implementation of SMOPE using RA-PSO is found to have a slight advantage over its implementation using S-PSO.

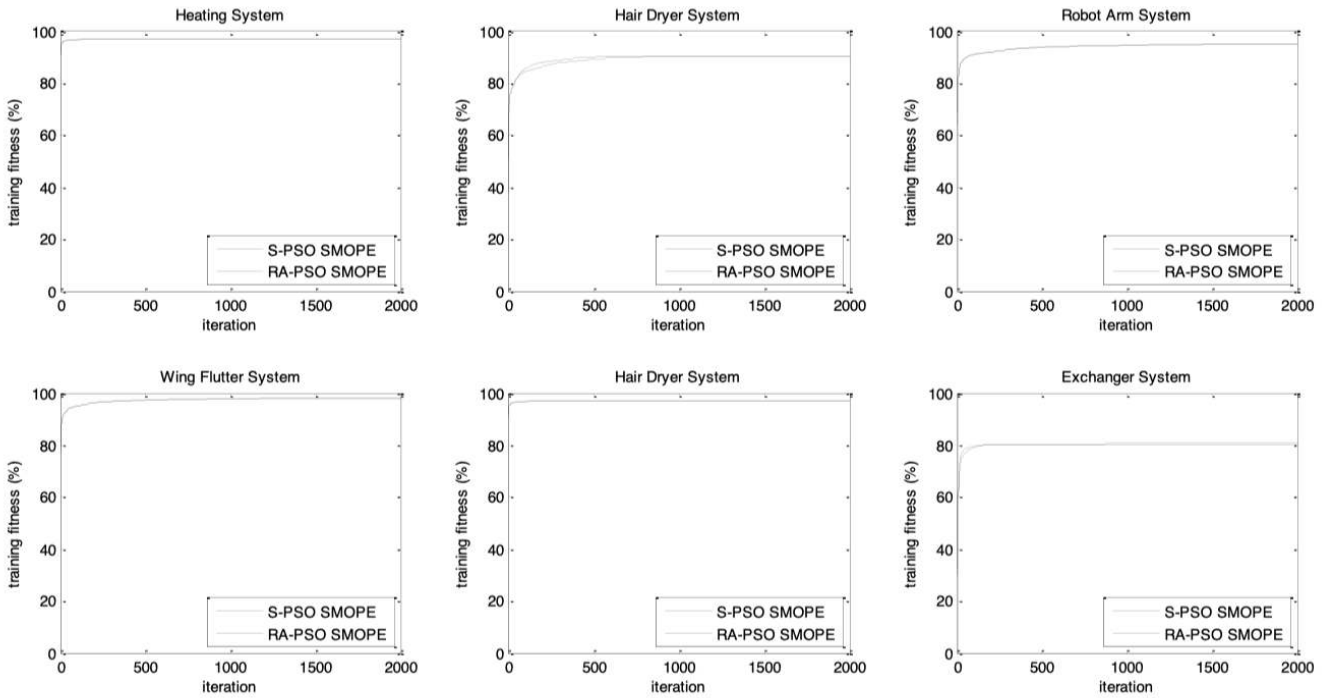


Figure 6. Convergence curves.

	S-PSO based SMOPE	RA-PSO based SMOPE-PSO
Heating System	$G_8(Z) = \frac{1.1728E - 01Z^{-1} + 1.2558E - 01Z^{-2}}{1 - 1.5447E + 00Z^{-1} + 5.1517E - 01Z^{-2} + 4.0880E - 02Z^{-3}}$	$G_7(Z) = \frac{2.0558E - 01 Z^{-1}}{1 - 1.6480E + 00 Z^{-1} + 4.2510E - 01Z^{-2} + 4.7193E - 01Z^{-3} - 2.3945E - 01Z^{-4}}$
Hair Dryer System	$G_{10}(Z) = \frac{1.9353E - 03Z^{-1} + 3.4780E - 03Z^{-2} + 6.3246E - 02Z^{-3} - 2.4032E + 00Z^{-4}}{1 - 1.0969E + 00Z^{-1} + 4.9053E - 02Z^{-2} + 2.4258E - 01Z^{-3} - 6.5639E - 02Z^{-4}}$	$G_{10}(Z) = \frac{-4.3221E - 04 Z^{-1} + 5.0368E - 03 Z^{-2} + 6.3328E - 02 Z^{-3} + 5.5303E - 02 Z^{-4}}{1 - 1.1112E + 00 Z^{-1} + 7.0820E - 02 Z^{-2} + 2.3274E - 01 Z^{-3} - 6.5128E - 02 Z^{-4}}$
Robot Arm System	$G_9(Z) = \frac{-6.2515E - 02Z^{-1} + 7.3661E - 02Z^{-2} - 2.6292E - 02Z^{-2}}{1 - 2.8196E + 00Z^{-1} + 3.6585E + 00Z^{-2} - 2.3624E + 00Z^{-3} + 6.7654E - 01Z^{-4}}$	$G_{28}(Z) = \frac{-5.8551E - 01 Z^{-1} + 1.3019E + 00 Z^{-2} - 1.2507E + 00Z^{-3} + 6.2992E - 01 Z^{-4} + 2.3527E - 02 Z^{-5} - 5.4968E - 02 Z^{-6} - 1.1418E - 01 Z^{-7} + 1.2279E + 00 Z^{-1} - 2.9497E - 01 Z^{-2} + 1.0180E + 00Z^{-3} + 4.5509E - 01Z^{-4} - 9.4178E - 01 Z^{-5} - 1.5290E - 01 Z^{-6} + 5.6338E - 01 Z^{-7}}{1 - 1.2279E + 00 Z^{-1} - 2.9497E - 01 Z^{-2} + 1.0180E + 00Z^{-3} + 4.5509E - 01Z^{-4} - 9.4178E - 01 Z^{-5} - 1.5290E - 01 Z^{-6} + 5.6338E - 01 Z^{-7}}$
Wing Flutter	$G_4(Z) = \frac{-3.3964E - 02Z^{-1}}{1 - 2.6113E + 00Z^{-1} + 2.4575E + 00Z^{-2} - 8.3518E - 01Z^{-3}}$	$G_{16}(Z) = \frac{-4.6148E - 02 Z^{-1}}{1 - 2.2871E + 00 Z^{-1} + 1.4704E + 00 Z^{-2} + 3.3797E - 01 Z^{-3} - 5.9775E - 01 Z^{-4} + 5.0341E - 02 Z^{-5} + 4.1748E - 02Z^{-6}}$
Ball Beam	$G_{24}(Z) = \frac{-2.7357E - 01Z^{-1} + 1.5260E - 01Z^{-2} + 2.9661E - 01Z^{-3}}{1 - 9.1080E - 01Z^{-1} - 2.8977E - 01Z^{-2} + 6.4964E - 02Z^{-3} - 1.0381E - 01Z^{-4} + 2.8406E - 02Z^{-5} + -2.0432E - 02Z^{-6} + 2.2931E - 01Z^{-7}}$	$G_{25}(Z) = \frac{-1.9259E - 01 Z^{-1} + 1.3219E - 01 Z^{-2} + 1.2913E - 01 Z^{-3} + 9.9303E - 02 Z^{-4}}{1 - 9.9073E - 01 Z^{-1} - 2.1849E - 01 Z^{-2} + 1.0525E - 01Z^{-3} - 1.3891E - 01 Z^{-4} + 5.4615E - 02 Z^{-5} - 1.2018E - 02 Z^{-6} + 1.9815E - 01 Z^{-7}}$
Exchanger System	$G_2(Z) = \frac{2.2076E - 01Z^{-1}}{1 - 1.2569E + 00Z^{-1} + 2.5761E - 01Z^{-2}}$	$G_2(Z) = \frac{2.3113E - 01 Z^{-1}}{1 - 1.2661E + 00 Z^{-1} + 2.6692E - 01 Z^{-2}}$

Figure 7. Mathematical models.

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